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PATENT COOPERATION TREATY

PCT

NOTIFICATION OF THE RECORDING OF A CHANGE

(PCT Rule 92bis.1 and
Administrative Instructions, Section 422)

From the INTERNATIONAL BUREAU

To:

NOONAN, Greg
Freehills Carter Smith & Beadle
101 Collins Street
Melbourne, VIC 3000
AUSTRALIE

Date of mailing (day/month/year) 15 June 2000 (15.06.00)	
Applicant's or agent's file reference 40129739	IMPORTANT NOTIFICATION
International application No. PCT/AU99/00409	International filing date (day/month/year) 26 May 1999 (26.05.99)

1. The following indications appeared on record concerning: <input type="checkbox"/> the applicant <input type="checkbox"/> the inventor <input checked="" type="checkbox"/> the agent <input type="checkbox"/> the common representative			
Name and Address NOONAN, Greg Freehills Patent Attorneys 101 Collins Street, Level 47 Melbourne, VIC 3000 Australia	State of Nationality	State of Residence	Telephone No. 03 9288 1577 Facsimile No. 03 9288 1567 Teleprinter No.
2. The International Bureau hereby notifies the applicant that the following change has been recorded concerning: <input checked="" type="checkbox"/> the person <input checked="" type="checkbox"/> the name <input checked="" type="checkbox"/> the address <input type="checkbox"/> the nationality <input type="checkbox"/> the residence			
Name and Address NOONAN, Greg Freehills Carter Smith & Beadle 101 Collins Street Melbourne, VIC 3000 Australia	State of Nationality	State of Residence	Telephone No. 03 9288 1577 Facsimile No. 03 9288 1567 Teleprinter No.
3. Further observations, if necessary:			
4. A copy of this notification has been sent to: <div style="display: flex; justify-content: space-between;"> <div> <input checked="" type="checkbox"/> the receiving Office <input checked="" type="checkbox"/> the International Searching Authority <input checked="" type="checkbox"/> the International Preliminary Examining Authority </div> <div> <input checked="" type="checkbox"/> the designated Offices concerned <input checked="" type="checkbox"/> the elected Offices concerned <input type="checkbox"/> other: </div> </div>			

The International Bureau of WIPO 34, chemin des Colombettes 1211 Geneva 20, Switzerland Facsimile No.: (41-22) 740.14.35	Authorized officer R. Raissi Telephone No.: (41-22) 338.83.38
--	--

PATENT COOPERATION TREATY

PCT

NOTIFICATION OF ELECTION

(PCT Rule 61.2)

From the INTERNATIONAL BUREAU

To:

Assistant Commissioner for Patents
United States Patent and Trademark
Office
Box PCT
Washington, D.C.20231
ÉTATS-UNIS D'AMÉRIQUE

in its capacity as elected Office

Date of mailing (day/month/year)
18 January 2000 (18.01.00)

International application No.
PCT/AU99/00409

Applicant's or agent's file reference
40129739

International filing date (day/month/year)
26 May 1999 (26.05.99)

Priority date (day/month/year)
26 May 1998 (26.05.98)

Applicant

ARMSTRONG, Jean

1. The designated Office is hereby notified of its election made:



in the demand filed with the International Preliminary Examining Authority on:

23 December 1999 (23.12.99)



in a notice effecting later election filed with the International Bureau on:

2. The election ☒ was

was not

made before the expiration of 19 months from the priority date or, where Rule 32 applies, within the time limit under Rule 32.2(b).

The International Bureau of WIPO
34, chemin des Colombettes
1211 Geneva 20, Switzerland

Facsimile No.: (41-22) 740.14.35

Authorized officer

Olivia RANAIVOJAONA

Telephone No.: (41-22) 338.83.38

The demand must be filed directly with the competent International Preliminary Examining Authority or, if two or more Authorities are competent, with the one chosen by the applicant. The full name or two-letter code of that Authority may be indicated by the applicant on the line below:

IPEA/ _____

PCT

CHAPTER II

DEMAND

under Article 31 of the Patent Cooperation Treaty:

The undersigned requests that the international application specified below be the subject of international preliminary examination according to the Patent Cooperation Treaty and hereby elects all eligible States (except where otherwise indicated).

For International Preliminary Examining Authority use only	
Identification of IPEA	Date of receipt of DEMAND
Box No. I IDENTIFICATION OF THE INTERNATIONAL APPLICATION	
Applicant's or agent's file reference	
International application No. PCT/AU99/00409	International filing date (day/month/year) 26 May 1999 26/05/99
(Earliest) Priority date (day/month/year) 26 May 1998 26/05/98	
Title of invention Data transmission and reception in multicarrier modulation systems	
Box No. II APPLICANT(S)	
Name and address: (Family name followed by given name; for a legal entity, full official designation. The address must include postal code and name of country.) ARMSTRONG, Jean 44 Longview Road North Balwyn, Victoria 3104 Australia	Telephone No.: Facsimile No.: Teleprinter No.:
State (that is, country) of nationality: Australia	State (that is, country) of residence: Australia
Name and address: (Family name followed by given name; for a legal entity, full official designation. The address must include postal code and name of country.)	
State (that is, country) of nationality:	State (that is, country) of residence:
Name and address: (Family name followed by given name; for a legal entity, full official designation. The address must include postal code and name of country.)	
State (that is, country) of nationality:	State (that is, country) of residence:
Name and address: (Family name followed by given name; for a legal entity, full official designation. The address must include postal code and name of country.)	
State (that is, country) of nationality:	State (that is, country) of residence:
<input type="checkbox"/> Further applicants are indicated on a continuation sheet.	

Box No. III AGENT OR COMMON REPRESENTATIVE; OR ADDRESS FOR CORRESPONDENCE

The following person is ☒ agent ☐ common representative
 and ☒ has been appointed earlier and represents the applicant(s) also for international preliminary examination.
☐ is hereby appointed and any earlier appointment of (an) agent(s)/common representative is hereby revoked.
☐ is hereby appointed, specifically for the procedure before the International Preliminary Examining Authority, in addition to the agent(s)/common representative appointed earlier.

Name and address: (Family name followed by given name; for a legal entity, full official designation.
 The address must include postal code and name of country.)

NOONAN, Greg
 CHERRY, James
 DI GIANTOMASSO, Frank
 CALLINAN, Keith
 JONES, Paul
 DAVY, John
 TULLOCH, Debra

Freehills Patent Attorneys
 Level 47
 101 Collins Street
 Melbourne, Victoria 3000
 AUSTRALIA

Telephone No.:

(613) 9288 1577

Facsimile No.:

(613) 9288 1567

Teleprinter No.:

☐ Address for correspondence: Mark this check-box where no agent or common representative is/has been appointed and the space above is used instead to indicate a special address to which correspondence should be sent.

Box No. IV BASIS FOR INTERNATIONAL PRELIMINARY EXAMINATION**Statement concerning amendments:***

1. The applicant wishes the international preliminary examination to start on the basis of:

☒ the international application as originally filed

the description ☐ as originally filed

☐ as amended under Article 34

the claims ☐ as originally filed

☐ as amended under Article 19 (together with any accompanying statement)

☐ as amended under Article 34

the drawings ☐ as originally filed

☐ as amended under Article 34

2. ☐ The applicant wishes any amendment to the claims under Article 19 to be considered as reversed.

3. ☐ The applicant wishes the start of the international preliminary examination to be postponed until the expiration of 20 months from the priority date unless the International Preliminary Examining Authority receives a copy of any amendments made under Article 19 or a notice from the applicant that he does not wish to make such amendments (Rule 69.1(d)). (This check-box may be marked only where the time limit under Article 19 has not yet expired.)

* Where no check-box is marked, international preliminary examination will start on the basis of the international application as originally filed or, where a copy of amendments to the claims under Article 19 and/or amendments of the international application under Article 34 are received by the International Preliminary Examining Authority before it has begun to draw up a written opinion or the international preliminary examination report, as so amended.

Language for the purposes of international preliminary examination: ENGLISH

☒ which is the language in which the international application was filed.

☐ which is the language of a translation furnished for the purposes of international search.

☐ which is the language of publication of the international application.

☐ which is the language of the translation (to be) furnished for the purposes of international preliminary application.

Box No. V ELECTION OF STATES

The applicant hereby elects all eligible States (that is, all States which have been designated and which are bound by Chapter II of the PCT)

excluding the following States which the applicant wishes not to elect:

Box No. VI CHECK LIST

The demand is accompanied by the following elements, in the language referred to in Box No. IV, for the purposes of international preliminary examination:

- | | | | |
|----|---|---|--------|
| 1. | translation of international application | : | sheets |
| 2. | amendments under Article 34 | : | sheets |
| 3. | copy (or, where required, translation) of amendments under Article 19 | : | sheets |
| 4. | copy (or, where required, translation) of statement under Article 19 | : | sheets |
| 5. | letter | : | sheets |
| 6. | other (<i>specify</i>) | : | sheets |

For International Preliminary Examining Authority use only

received not received

<input type="checkbox"/>	<input type="checkbox"/>
<input type="checkbox"/>	<input type="checkbox"/>
<input type="checkbox"/>	<input type="checkbox"/>
<input type="checkbox"/>	<input type="checkbox"/>
<input type="checkbox"/>	<input type="checkbox"/>
<input type="checkbox"/>	<input type="checkbox"/>

The demand is also accompanied by the item(s) marked below:

- | | |
|--|---|
| 1. <input type="checkbox"/> fee calculation sheet | 4. <input type="checkbox"/> statement explaining lack of signature |
| 2. <input type="checkbox"/> separate signed power of attorney | 5. <input type="checkbox"/> nucleotide and or amino acid sequence listing in computer readable form |
| 3. <input type="checkbox"/> copy of general power of attorney; reference number if any | 5. <input type="checkbox"/> other (<i>specify</i>): |

Box No. VII SIGNATURE OF APPLICANT, AGENT OR COMMON REPRESENTATIVE

Next to each signature, indicate the name of the person signing and the capacity in which the person signs (if such capacity is not obvious from reading the demand).

.....
**Greg Noonan, agent for and on behalf of
 Jean Armstrong**

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- | | | |
|----|---|---|
| 1. | Date of actual receipt of DEMAND: | |
| 2. | Adjusted date of receipt of demand due to CORRECTIONS under Rule 60.1(b): | |
| 3. | <input type="checkbox"/> The date of receipt of the demand is AFTER the expiration of 19 months from the priority date and item 4 or 5, below, does not apply. | <input type="checkbox"/> The applicant has been informed accordingly. |
| 4. | <input type="checkbox"/> The date of receipt of the demand is WITHIN the period of 19 months from the priority date as extended by virtue of Rule 80.5. | |
| 5. | <input type="checkbox"/> Although the date of receipt of the demand is after the expiration of 19 months from the priority date, the delay in arrival is EXCUSED pursuant to Rule 82. | |

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Demand received from IPEA on:

PCT REQUEST

40129739

Original (for SUBMISSION) - printed on 26.05.1999 02:25:08 PM

0	For receiving Office use only	
0-1	International Application No.	
0-2	International Filing Date	
0-3	Name of receiving Office and "PCT International Application"	
0-4 0-4-1	Form - PCT/RO/101 PCT Request Prepared using	PCT-EASY Version 2.83 (updated 01.03.1999)
0-5	Petition The undersigned requests that the present international application be processed according to the Patent Cooperation Treaty	
0-6	Receiving Office (specified by the applicant)	Australian Patent Office (RO/AU)
0-7	Applicant's or agent's file reference	40129739
I	Title of invention	DATA TRANSMISSION AND RECEPTION IN MULTICARRIER MODULATION SYSTEMS
II	Applicant	
II-1	This person is:	applicant and inventor
II-2	Applicant for	all designated States
II-4	Name (LAST, First)	ARMSTRONG, Jean
II-5	Address:	44 Longview Road North Balwyn, Victoria 3104 Australia
II-6	State of nationality	AU
II-7	State of residence	AU
IV-1	Agent or common representative; or address for correspondence The person identified below is hereby/has been appointed to act on behalf of the applicant(s) before the competent International Authorities as:	agent
IV-1-1	Name	FREEHILLS PATENT ATTORNEYS
IV-1-2	Address:	NOONAN, Greg CALLINAN, Keith CHERRY, James JONES, Paul Level 47 101 Collins Street Melbourne, Victoria 3000 Australia
IV-1-3	Telephone No.	(03) 9288 1577
IV-1-4	Facsimile No.	(03) 9288 1567

PCT REQUEST

40129739

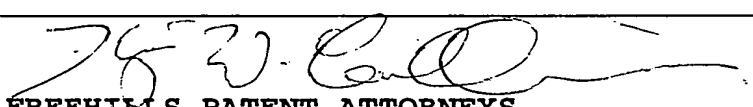
Original (for SUBMISSION) - printed on 26.05.1999 02:25:08 PM

V	Designation of States	
V-1	Regional Patent (other kinds of protection or treatment, if any, are specified between parentheses after the designation(s) concerned)	AP: GH GM KE LS MW SD SZ UG ZW and any other State which is a Contracting State of the Harare Protocol and of the PCT EA: AM AZ BY KG KZ MD RU TJ TM and any other State which is a Contracting State of the Eurasian Patent Convention and of the PCT EP: AT BE CH&LI CY DE DK ES FI FR GB GR IE IT LU MC NL PT SE and any other State which is a Contracting State of the European Patent Convention and of the PCT OA: BF BJ CF CG CI CM GA GN GW ML MR NE SN TD TG and any other State which is a member State of OAPI and a Contracting State of the PCT
V-2	National Patent (other kinds of protection or treatment, if any, are specified between parentheses after the designation(s) concerned)	AE AL AM AT AU AZ BA BB BG BR BY CA CH&LI CN CU CZ DE DK EE ES FI GB GD GE GH GM HR HU ID IL IN IS JP KE KG KP KR KZ LC LK LR LS LT LU LV MD MG MK MN MW MX NO NZ PL PT RO RU SD SE SG SI SK SL TJ TM TR TT UA UG US UZ VN YU ZA ZW
V-5	Precautionary Designation Statement In addition to the designations made under items V-1, V-2 and V-3, the applicant also makes under Rule 4.9(b) all designations which would be permitted under the PCT except any designation(s) of the State(s) indicated under item V-6 below. The applicant declares that those additional designations are subject to confirmation and that any designation which is not confirmed before the expiration of 15 months from the priority date is to be regarded as withdrawn by the applicant at the expiration of that time limit.	
V-6	Exclusion(s) from precautionary designations	NONE
VI-1	Priority claim of earlier national application	
VI-1-1	Filing date	26 May 1998 (26.05.1998)
VI-1-2	Number	PP3698
VI-1-3	Country	AU
VI-2	Priority claim of earlier national application	
VI-2-1	Filing date	22 June 1998 (22.06.1998)
VI-2-2	Number	PP4250
VI-2-3	Country	AU

PCT REQUEST

40129739

Original (for SUBMISSION) - printed on 26.05.1999 02:25:08 PM

VI-3	Priority document request The receiving Office is requested to prepare and transmit to the International Bureau a certified copy of the earlier application(s) identified above as item(s):	VI-1, VI-2	
VII-1	International Searching Authority Chosen	Australian Patent Office (ISA/AU)	
VIII	Check list	number of sheets	electronic file(s) attached
VIII-1	Request	3	-
VIII-2	Description	23	-
VIII-3	Claims	5	-
VIII-4	Abstract	1	91460128.txt
VIII-5	Drawings	18	-
VIII-7	TOTAL	50	
	Accompanying items	paper document(s) attached	electronic file(s) attached
VIII-8	Fee calculation sheet	✓	-
VIII-16	PCT-EASY diskette	-	diskette
VIII-18	Figure of the drawings which should accompany the abstract	1	
VIII-19	Language of filing of the International application	English	
IX-1	Signature of applicant or agent		
IX-1-1	Name	FREEHILLS PATENT ATTORNEYS	
IX-1-2	Name of signatory	CALLINAN, Keith	

FOR RECEIVING OFFICE USE ONLY

10-1	Date of actual receipt of the purported International application	
10-2	Drawings:	
10-2-1	Received	
10-2-2	Not received	
10-3	Corrected date of actual receipt due to later but timely received papers or drawings completing the purported International application	
10-4	Date of timely receipt of the required corrections under PCT Article 11(2)	
10-5	International Searching Authority	ISA/AU
10-6	Transmittal of search copy delayed until search fee is paid	

FOR INTERNATIONAL BUREAU USE ONLY


11-1	Date of receipt of the record copy by the International Bureau	
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INTERNATIONAL PRELIMINARY EXAMINATION REPORT

(PCT Article 36 and Rule 70)

Applicant's or agent's file reference 40129739	FOR FURTHER ACTION	See Notification of Transmittal of International Preliminary Examination Report (Form PCT/IPEA/416).
International application No. PCT/AU99/00409	International filing date (day/month/year) 26 May 1999	Priority Date (day/month/year) 26 May 1998
International Patent Classification (IPC) or national classification and IPC Int. Cl. ⁷ H04J 11/00; 13/00; H04B 7/204; H04L 27/00		
Applicant ARMSTRONG, Jean		

1.	This international preliminary examination report has been prepared by this International Preliminary Examining Authority and is transmitted to the applicant according to Article 36.	
2.	This REPORT consists of a total of 4 sheets, including this cover sheet. <input checked="" type="checkbox"/> This report is also accompanied by ANNEXES, i.e., sheets of the description, claims and/or drawings which have been amended and are the basis for this report and/or sheets containing rectifications made before this Authority (see Rule 70.16 and Section 607 of the Administrative Instructions under the PCT). These annexes consist of a total of 12 sheet(s).	
3.	This report contains indications relating to the following items: I <input checked="" type="checkbox"/> Basis of the report II <input type="checkbox"/> Priority III <input type="checkbox"/> Non-establishment of opinion with regard to novelty, inventive step and industrial applicability IV <input checked="" type="checkbox"/> Lack of unity of invention V <input checked="" type="checkbox"/> Reasoned statement under Article 35(2) with regard to novelty, inventive step or industrial applicability; citations and explanations supporting such statement VI <input type="checkbox"/> Certain documents cited VII <input type="checkbox"/> Certain defects in the international application VIII <input type="checkbox"/> Certain observations on the international application	

Date of submission of the demand 23 December 1999	Date of completion of the report 26 September 2000
Name and mailing address of the IPEA/AU AUSTRALIAN PATENT OFFICE PO BOX 200, WODEN ACT 2606, AUSTRALIA E-mail address: pct@ipaaustralia.gov.au Facsimile No. (02) 6285 3929	Authorized Officer  ROBERT BARTRAM Telephone No. (02) 6283 2215

I. Basis of the report

1. With regard to the elements of the international application:*
- ☐ the international application as originally filed.
- ☒ the description, pages 1 to 8, 12 to 17, 19 to 21, and 23 as originally filed,
pages , filed with the demand,
pages 9 to 11, 18, and 22, received on 6 June 2000 with the letter of the same
- ☒ the claims, pages , as originally filed,
pages , as amended (together with any statement) under Article 19,
pages , filed with the demand,
pages 24 to 30, received on 6 June 2000 with the letter of the same
- ☒ the drawings, pages 1/18 to 18/18, as originally filed,
pages , filed with the demand,
pages , received on with the letter of
- ☐ the sequence listing part of the description:
pages , as originally filed
pages , filed with the demand
pages , received on with the letter of
2. With regard to the language, all the elements marked above were available or furnished to this Authority in the language in which the international application was filed, unless otherwise indicated under this item.
These elements were available or furnished to this Authority in the following language which is:
- ☐ the language of a translation furnished for the purposes of international search (under Rule 23.1(b)).
- ☐ the language of publication of the international application (under Rule 48.3(b)).
- ☐ the language of the translation furnished for the purposes of international preliminary examination (under Rules 55.2 and/or 55.3).
3. With regard to any nucleotide and/or amino acid sequence disclosed in the international application, was on the basis of the sequence listing:
- ☐ contained in the international application in written form.
- ☐ filed together with the international application in computer readable form.
- ☐ furnished subsequently to this Authority in written form.
- ☐ furnished subsequently to this Authority in computer readable form.
- ☐ The statement that the subsequently furnished written sequence listing does not go beyond the disclosure in the international application as filed has been furnished.
- ☐ The statement that the information recorded in computer readable form is identical to the written sequence listing has been furnished
4. ☐ The amendments have resulted in the cancellation of:
- ☐ the description, pages
- ☐ the claims, Nos.
- ☐ the drawings, sheets/fig.
5. ☐ This report has been established as if (some of) the amendments had not been made, since they have been considered to go beyond the disclosure as filed, as indicated in the Supplemental Box (Rule 70.2(c)).**

* Replacement sheets which have been furnished to the receiving Office in response to an invitation under Article 14 are referred to in this report as "originally filed" and are not annexed to this report since they do not contain amendments (Rules 70.16 and 70.17).

** Any replacement sheet containing such amendments must be referred to under item 1 and annexed to this report

IV. Lack of unity of invention

1. In response to the invitation to restrict or pay additional fees the applicant has:

- ☐ restricted the claims.
- ☐ paid additional fees.
- ☐ paid additional fees under protest.
- ☐ neither restricted nor paid additional fees.

2. ☐ This Authority found that the requirement of unity of invention is not complied with and chose, according to Rule 68.1, not to invite the applicant to restrict or pay additional fees.

3. This Authority considers that the requirement of unity of invention in accordance with Rules 13.1, 13.2 and 13.3 is

- ☐ complied with.
- ☒ not complied with for the following reasons:

Claims 1, 2, 4 to 35, and 37 to 41 are directed towards the modulation including a weighting operation before inverse transformation. It is considered that the use of weighting operations before inverse transformation comprises a "first special technical feature".

Claims 3 and 36 are directed towards the modulation involving a windowing operation in which the data is multiplied with a complex window after inverse transformation. It is considered that the use of a windowing operation after inverse transformation comprises a "second special technical feature".

Since the above mentioned groups of claims do not share any of the technical features identified, a technical relationship between the inventions does not appear to exist. Accordingly the claims do not relate to one invention only or to a single inventive concept.

As a search was conducted without extra effort justifying additional fees the examination was also able to be provided for all of the claims.

4. Consequently, the following parts of the international application were the subject of international preliminary examination in establishing this report:

- ☒ all parts.
- ☐ the parts relating to claims Nos.

V. Reasoned statement under Article 35(2) with regard to novelty, inventive step or industrial applicability; citations and explanations supporting such statement**1. Statement**

Novelty (N)	Claims 1 to 41	YES
	Claims	NO
Inventive step (IS)	Claims 1 to 41	YES
	Claims	NO
Industrial applicability (IA)	Claims 1 to 41	YES
	Claims	NO

2. Citations and explanations (Rule 70.7)

D1 - US 5 416 777

D2 - US 5 559 834

Claims 1,2, 4-35, and 37 - 41 are considered to satisfy the criteria for novelty and inventiveness in that these claims define the use of a weighting operation before the inverse transformation. Neither document D1 or D2 discloses the use of a weighting operation before the inverse transformation.

Claims 3 and 36 define the use of a complex windowing operation after inverse transformation. This feature is not disclosed in document D1 or D2. D1 does disclose multiplying with areal window function as opposed to your invention of "complex windowing". The use of complex windowing has not been achieved or disclosed in this existing art.

11. The output of the ADC 11 provides receiver aggregate data r_k is input to a serial-to-parallel converter 12 that provides receiver transform input data $x_{0,i} \dots x_{N-1,i}$ to an orthogonal transform 16. The orthogonal transform 16 then provides output data $e_{0,i} \dots e_{N-1,i}$ that corresponds with the input data $d_{0,i} \dots d_{N-1,i}$.
- 5 In the prior art as in embodiments of the invention, the orthogonal transforms 3 and 16 in the transmitter and receiver respectively, are the inverse of each other. Conceptually, it is considered that the orthogonal transform 3 in the transmitter is an inverse transform to provide a mapping from the frequency domain to the time domain and the orthogonal transform 16 in the receiver is a forward transform to
- 10 provide a mapping from the time domain back to the frequency domain.

In an ideal system, the output data $e_{0,i} \dots e_{N-1,i}$ is precisely equal to the input data $d_{0,i} \dots d_{N-1,i}$. However, as previously outlined, this is not the case in practical systems as are known in the prior art.

- In an OFDM receiver, the analog reception signal $v(t)$ is translated down to baseband to produce the receiver baseband signal $r(t)$. If the other carriers all beat down to frequencies that, in the time domain, have a whole number of cycles in the symbol period (T), there is zero contribution from all these other subcarriers. Thus the subcarriers are mathematically orthogonal if the subcarrier spacing is a multiple of $1/T$. This condition is a natural result of using an orthogonal transform pair 3 and 16 such as a IDFT and DFT in the transmitter and receiver respectively.
- 15
- 20

Known OFDM systems such as that described above, are deficient as earlier outlined. Fig. 2 demonstrates the power spectra of an OFDM signal which demonstrates the lack of bandwidth containment of the known OFDM system shown in Fig. 1.

- 25 Fig. 3 is a graph of complex interference coefficients ($C_0 \dots C_{N-1}$) for illustrative values of frequency offset ($\Delta f T = 0.2$ and $N = 16$, with phase-offset equal to zero at the beginning of the symbol period). Frequency offset Δf can arise due to absolute differences in the frequencies f_c and f_r of local oscillators in the transmitter and receiver respectively, and by Doppler shifts due to relative motion

of transmitter and receiver. Frequency offset results in ICI, which is quantitatively indicated by complex interference factors.

In Fig. 3, real components of the complex interference coefficients are represented by diamonds and the imaginary components are represented by triangles. ICI may be interpreted in terms of the complex interference coefficients ($C_0 \dots C_{N-1}$) that measure the contribution of a transmitter subcarrier to each demodulated subcarrier; that is, the interference in one subcarrier arising from effects between subcarriers.

As can be seen from Fig. 3, the complex interference coefficients ($C_0 \dots C_{N-1}$) vary smoothly between subcarriers except at the transitions from the reference subcarrier (whose impact on other subcarriers is being measured) to its immediately adjacent subcarriers.

It is observed that the form of variation of complex interference coefficients ($C_0 \dots C_{N-1}$) across subcarriers can be closely modelled by a relatively low order polynomial equation. This predicability allows for generally consistent cancellation of ICI by modulating groups of subcarriers with representations of the data.

An example embodiment of the invention is now described in relation to Fig. 4 and Fig. 5.

Fig. 4 shows a transmitter in accordance with an embodiment of the invention. Compared with the OFDM system shown in Fig. 1, the transmitter shown in Fig. 4 provides for modulating representations of data on groups of subcarriers, and introducing a substantially predetermined amount of intersymbol interference between symbols.

The input data ($d_{0,i} \dots d_{D-1,i}$) is provided on input data channels. Representations of the input data are modulated onto groups of subcarriers by multiplying each input data through a weighting means 1 to provide weighted input data which is then input to an orthogonal transform 3. In Fig. 4, the weighting means 1 includes what are represented as a collection of the transmitter weighting coefficients (p_0 and

p_1). Each input data ($d_{0,i} \dots d_{D-1,i}$) on the input data channels is multiplied by transmitter weighting coefficients (p_0 and p_1) in order to generate two weighted representations of each of the input data ($d_{0,i} \dots d_{D-1,i}$). Collectively these weighted representations of the input data ($d_{0,i} \dots d_{D-1,i}$) are the weighted input data ($a_{0,i} \dots a_{N-1,i}$) which are used to modulate two adjacent subcarriers. It is not necessary that every subcarrier be used. (For example, in baseband applications, it is necessary that the input to the transform have Hermitian symmetry so that the output has no imaginary components.) Rather, every subcarrier should be paired with an oppositely weighted subcarrier. Preferably, paired subcarriers are adjacent to each other.

The orthogonal transform 3 has N inputs that directly correspond with the number of subcarriers N modulated by representations of the input data, in this case the weighted input data. Each output of the orthogonal transform 3 in the transmitter corresponds with a transmitter transform output data channel.

Fig. 5 shows the interaction of a delay means 6 and the parallel-to-serial converter 7. Half of the transmitter transform output data from the orthogonal transform 3 is passed to a delay means 6 which together with parallel-to-serial converter 7 and the addition operation introduces a known and predetermined amount of intersymbol interference between symbols. The first $N/2$ elements of the transmitter transform output data are converted to serial form, while the second $N/2$ elements are first delayed by $T/2$ before parallel-to-serial conversion. Each delayed output data is summed with a non delayed output, so that each transmitter aggregate data is the summation of two samples from adjacent symbols.

Accordingly, each transmitter aggregate data is the summation of two terms from adjacent symbols. The table below shows the relationship between the aggregate data and the transmitter transform output data for an overlap of $T/2$.

provides a cyclic extension 4 of $N/2$ points. Again the complex window 5 is of the form $[1 - \exp(j2\pi \cdot l/N)]$.

In both cases, the complex window 5, of the form $[1 - \exp(j2\pi \cdot l/N)]$, acts to multiply the l -th value of the transmitter transform output data by a factor of $[1 - \exp(j2\pi \cdot l/N)]$ before further processing.

The cyclic contraction required in the receiver is preferably achieved by simply performing an element-by-element summation of the data points indexed $0 \dots N/2 - 1$ with those data points indexed $N/2 \dots N - 1$. In this case, the number of data values is doubled and then halved by the cyclic extension 4 and cyclic contraction 10 14 respectively.

In both cases, the exponential roll-off window 13 in the receiver are preferably the complex conjugate the exponential roll-off window 5 in the transmitter.

The embodiments described above modulate the subcarriers with representations of the input data that are respectively equal positive and negative values of each input data. However, it is possible and in some cases desirable (such, as in the 15 presence of strong multipath interference) to use higher order schemes which use a greater number of representations of the input data.

By extension of the transmitter and receiver shown in Figs. 4 and 6 respectively, cubic cancellation can be achieved by using with the following transmitter 20 weighting and receiver weighting coefficients:

$$p_0 = 1, p_1 = -2, p_2 = 1$$

$$q_0 = 1, q_1 = -2, q_2 = 1$$

This corresponds with the polynomial:

$$1 - 2x - x^2$$

Fig. 16 is a scatterplot of symbols received for an embodiment that uses 64 subcarriers and cubic cancellation.

Fig. 17 is a graph showing the signal to ICI noise ratio of an embodiment of the invention compared with the signal to ICI noise ratio of a conventional OFDM system.

Fig. 18 includes two graphs - an upper graph showing the power spectrum roll-off of a conventional OFDM system, and a lower graph showing the power spectrum roll-off of a typical embodiment.

OFDM systems can use various different schemes to modulate subcarriers, such as phase shift keying (PSK) or quadrature amplitude modulation (QAM). Embodiments of the invention do not depend on the mapping of data to be transmitted to input data ($d_{0,i} \dots d_{D-1,i}$) and are therefore applicable to forms of modulation that can be used with OFDM generally.

Preferably a Fourier-based frequency transform, such as a DFT, or a discrete cosine or sine transform (DCT or DST) is used in the described embodiments. However, it is not necessary that an orthogonal transform be of this type as there are a number of other orthogonal transforms that may also be suitable, such as the Walsh transform, the Hadamard transform and the various types of wavelet transforms.

The orthogonal transform can in certain embodiments make use of fact that data which modulates particular subcarriers is correlated, and similarly in the receiver it is the weighted and summed outputs that are important. Consequently, the computational complexity involved in transformation calculations can be significantly reduced by the use of appropriate algorithms which assume that certain data points are correlated.

This involves appropriate exploitation of techniques for reducing the complexity of Fast Fourier Transform (FFT) calculations, for example, the decimation in time and decimation in frequency algorithms.

THE CLAIMS DEFINING THE INVENTION ARE AS FOLLOWS

1. A method of transmitting data in a multicarrier modulation system in which transform pairs allow communication using multiple subcarriers, the method including:

5 modulating representations of data on groups of subcarriers; and

 introducing a predetermined amount of intersymbol interference between symbols.

2. A method as claimed in claim 1 wherein the groups of subcarriers include non-overlapping sets of M adjacent subcarriers, and the M respective representations
10 are integer multiples of the data, the integers corresponding with coefficients of the expanded polynomial expression $(1-x)^{M-1}$.

3. A method as claimed in any one of claims 1 or 2 wherein the data is modulated on a pair of adjacent subcarriers, and the representations of the data are multiples of 1 and -1.

15 4. A method as claimed in any one of claims 1 to 3 wherein introducing intersymbol interference includes overlapping successive symbols to a predetermined extent by delaying and summing groups of samples of the symbols.

5. A method as claimed in claim 4 wherein successive symbols are overlapped with each other by half a symbol period.

20 6. A method as claimed in any one of claims 1 to 5 wherein the modulation includes a weighting operation in which the data is multiplied with weighting factors, before inverse transformation.

7. A method as claimed in any one of claims 1 to 5 wherein the modulation involves a windowing operation in which the data is multiplied with a window, after
25 inverse transformation.

8. A method as claimed in any one of claims 1 to 7 wherein inverse transformation includes using mathematical correlations between representations of the data to reduce computational and/or memory requirements of hardware on which the inverse transformation is determined.
- 5 9. A method as claimed in any one of claims 1 to 5 wherein subcarriers are modulated by a summation of representations of different data.
10. A method as claimed in claim 9 wherein each subcarrier is modulated by the difference between adjacent data.
11. A method as claimed in any one of claims 1 to 10 including providing pilot
10 tones on subcarriers.
12. A method as claimed in claim 11 wherein relative values of the pilot tones on successive symbols follows the sequence +1, 0, +1, 0, -1, 0, -1, 0.
13. A method of receiving data in a multicarrier modulation system in which transform pairs allow communication using multiple subcarriers, the method
15 including:
- demodulating data from representations of data on groups of subcarriers;
and
- removing a predetermined amount of intersymbol interference between symbols.
- 20 14. A method as claimed in claim 13 wherein the groups of subcarriers include non-overlapping sets of M adjacent subcarriers, and the M respective representations are integer multiples of the data, the integers corresponding with coefficients of the expanded polynomial expression $(1-x)^{M-1}$.
15. A method as claimed in any one of claims 13 or 14 wherein the data is
25 modulated on a pair of adjacent subcarriers, and the representations of the data

are multiples of 1 and -1.

16. A method as claimed in any one of claims 13 to 15 wherein the demodulation includes a weighting and summing operation in which the representations are multiplied with weighting factors, and the results summed, after transformation.

5 17. A method as claimed in any one of claims 13 to 15 wherein the demodulation includes a weighting and summing operation in which the representations are multiplied with weighting factors, and the results summed, as part of transformation.

10 18. A method as claimed in any one of claims 13 to 15 wherein the demodulation includes a windowing operation in which the representations are multiplied with a window, before transformation.

15 19. A method as claimed in any one of claims 13 to 18 wherein removing intersymbol interference between symbols includes removing a predetermined amount of intersymbol interference caused by overlapping symbols to a predetermined extent.

20. A method as claimed in claim 19 wherein the predetermined amount of intersymbol interference is caused by overlapping symbols by half a symbol period.

20 21. A method as claimed in any one of claims 13 to 20 wherein removing intersymbol interference between symbols includes delaying groups of samples so that each transformation operates on samples which reduce the error rate.

22. A method as claimed in any one of claims 13 to 20 wherein removing intersymbol interference between symbols includes frequency domain equalisation.

25 23. A method as claimed in claim 22 wherein frequency domain equalisation involves relatively few significant terms owing to the use of groups of subcarriers

modulated by representations of the data.

24. A method as claimed in claim 20 wherein removing intersymbol interference between symbols includes frequency domain equalisation in which the form of calculations involved are the same for each subcarrier.

5 25. A method as claimed in any one of claims 22 to 24 wherein frequency domain equalisation operates on the output of the demodulation.

26. A method as claimed in any one of claims 13 to 25 wherein removing intersymbol interference includes a fixed operation for removing intersymbol interference caused by introduction of a predetermined amount of intersymbol
10 interference, and an adaptive operation for removing intersymbol interference caused by reasons other than introduction of a predetermined amount of intersymbol interference.

27. A method as claimed in any one of claims 13 to 26 wherein transformation involves using mathematical correlations between representations of the data to
15 reduce computational and/or memory requirements of hardware on which the transformation is determined.

28. A method as claimed in any one of claims 13 to 27 including symbol synchronisation involving measuring the correlation between sections of signal, in which pilot tones are provided on subcarriers.

20 29. A method as claimed in claim 28 in which relative values of the pilot tones on successive symbols follows the sequence +1, 0, +1, 0, -1, 0, -1, 0.

30. A method as claimed in any one of claims 13 to 29 including frequency synchronisation involving measuring phase changes between the pilot tones provided on subcarriers.

25 31. A method as claimed in any one of claims 13 to 27 including frequency synchronisation involving calculating a metric having a known dependence on

frequency offset.

32. A method as claimed in any claim 31 wherein the metric approximates the multiplicative product of frequency offset and symbol period, and is calculated using the expression:

5
$$\operatorname{Re}\left(\frac{y_{k,i} + y_{k+1,i}}{y_{k,i} - y_{k+1,i}}\right)$$

33. A transmitter suitable for transmitting data in a multicarrier modulation system in which transform pairs allow communication using multiple subcarriers, the transmitter including:

means for modulating representations of data on groups of subcarriers; and

10 means for introducing a predetermined amount of intersymbol interference between symbols.

34. A receiver suitable for receiving data in a multicarrier modulation system in which transform pairs allow communication using multiple subcarriers, the receiver including:

15 means for demodulating data from representations of data on groups of subcarriers; and

means for removing a predetermined amount of intersymbol interference between symbols.

35. A multicarrier modulation system incorporating one or more transmitters as
20 claimed in claim 33 and one or more receivers as claimed in claim 34 wherein the transmitters and receivers are adapted to communicate with each other.

11. The output of the ADC 11 provides receiver aggregate data r_k which is input to a serial-to-parallel converter 12 that provides receiver transform input data $x_{0,i} \dots x_{N-1,i}$ to an orthogonal transform 16. The orthogonal transform 16 then provides output data $e_{0,i} \dots e_{N-1,i}$ that corresponds with the input data $d_{0,i} \dots d_{N-1,i}$.
- 5 In the prior art as in embodiments of the invention, the orthogonal transforms 3 and 16 in the transmitter and receiver respectively, are the inverse of each other. Conceptually, it is considered that the orthogonal transform 3 in the transmitter is an inverse transform to provide a mapping from the frequency domain to the time domain and the orthogonal transform 16 in the receiver is a forward transform to
- 10 provide a mapping from the time domain back to the frequency domain.

In an ideal system, the output data $e_{0,i} \dots e_{N-1,i}$ is precisely equal to the input data $d_{0,i} \dots d_{N-1,i}$. However, as previously outlined, this is not the case in practical systems as are known in the prior art.

- In an OFDM receiver, the analog reception signal $v(t)$ is translated down to baseband to produce the receiver baseband signal $r(t)$. If the other carriers all beat down to frequencies that, in the time domain, have a whole number of cycles in the symbol period (T), there is zero contribution from all these other subcarriers. Thus the subcarriers are mathematically orthogonal if the subcarrier spacing is a multiple of $1/T$. This condition is a natural result of using an orthogonal transform
- 15 pair 3 and 16 such as a IDFT and DFT in the transmitter and receiver respectively.
- 20

Known OFDM systems such as that described above, are deficient as earlier outlined. Fig. 2 demonstrates the power spectra of an OFDM signal which demonstrates the lack of bandwidth containment of the known OFDM system shown in Fig. 1.

- 25 Fig. 3 is a graph of complex interference coefficients ($C_0 \dots C_{N-1}$) for illustrative values of frequency offset ($\Delta fT = 0.2$ and $N = 16$, with phase-offset equal to zero at the beginning of the symbol period). Frequency offset Δf can arise due to absolute differences in the frequencies f_c and f_r of local oscillators in the transmitter and receiver respectively, and by Doppler shifts due to relative motion

of transmitter and receiver. Frequency offset results in ICI, which is quantitatively indicated by complex interference factors.

In Fig. 3, real components of the complex interference coefficients are represented by diamonds and the imaginary components are represented by triangles. ICI may be interpreted in terms of the complex interference coefficients ($C_0 \dots C_{N-1}$) that measure the contribution of a transmitter subcarrier to each demodulated subcarrier; that is, the interference in one subcarrier arising from effects between subcarriers.

As can be seen from Fig. 3, the complex interference coefficients ($C_0 \dots C_{N-1}$) vary smoothly between subcarriers except at the transitions from the reference subcarrier (whose impact on other subcarriers is being measured) to its immediately adjacent subcarriers.

It is observed that the form of variation of complex interference coefficients ($C_0 \dots C_{N-1}$) across subcarriers can be closely modelled by a relatively low order polynomial equation. This predictability allows for generally consistent cancellation of ICI by modulating groups of subcarriers with representations of the data.

An example embodiment of the invention is now described in relation to Fig. 4 and Fig. 5.

Fig. 4 shows a transmitter in accordance with an embodiment of the invention. Compared with the OFDM system shown in Fig. 1, the transmitter shown in Fig. 4 provides for modulating representations of data on groups of subcarriers, and introducing a substantially predetermined amount of intersymbol interference between symbols.

The input data ($d_{0,i} \dots d_{D-1,i}$) is provided on input data channels. Representations of the input data are modulated onto groups of subcarriers by multiplying each input data through a weighting means 1 to provide weighted input data which is then input to an orthogonal transform 3. In Fig. 4, the weighting means 1 includes what are represented as a collection of the transmitter weighting coefficients (p_0 and

p_1). Each input data ($d_{0,i} \dots d_{D-1,i}$) on the input data channels is multiplied by transmitter weighting coefficients (p_0 and p_1) in order to generate two weighted representations of each of the input data ($d_{0,i} \dots d_{D-1,i}$). Collectively these weighted representations of the input data ($d_{0,i} \dots d_{D-1,i}$) are the weighted input data ($a_{0,i} \dots$
 5 $a_{N-1,i}$) which are used to modulate two adjacent subcarriers. It is not necessary that every subcarrier be used. (For example, in baseband applications, it is necessary that the input to the transform have Hermitian symmetry so that the output has no imaginary components.) Rather, every subcarrier should be paired with an oppositely weighted subcarrier. Preferably, paired subcarriers are adjacent to each
 10 other.

The orthogonal transform 3 has N inputs that directly correspond with the number of subcarriers N modulated by representations of the input data, in this case the weighted input data. Each output of the orthogonal transform 3 in the transmitter corresponds with a transmitter transform output data channel.

15 Fig. 5 shows the interaction of a delay means 6 and the parallel-to-serial converter 7. Half of the transmitter transform output data from the orthogonal transform 3 is passed to a delay means 6 which together with parallel-to-serial converter 7 and the addition operation introduces a known and predetermined amount of intersymbol interference between symbols. The first $N/2$ elements of the
 20 transmitter transform output data are converted to serial form, while the second $N/2$ elements are first delayed by $T/2$ before parallel-to-serial conversion. Each delayed output data is summed with a non delayed output, so that each transmitter aggregate data is the summation of two samples from adjacent symbols.

25 Accordingly, each transmitter aggregate data is the summation of two terms from adjacent symbols. The table below shows the relationship between the aggregate data and the transmitter transform output data for an overlap of $T/2$.

provides a cyclic extension 4 of $N/2$ points. Again the complex window 5 is of the form $[1 - \exp(j2\pi \cdot l/N)]$.

In both cases, the complex window 5, of the form $[1 - \exp(j2\pi \cdot l/N)]$, acts to multiply the l -th value of the transmitter transform output data by a factor of $[1 - \exp(j2\pi \cdot l/N)]$ before further processing.

The cyclic contraction required in the receiver is preferably achieved by simply performing an element-by-element summation of the data points indexed $0 \dots N/2 - 1$ with those data points indexed $N/2 \dots N - 1$. In this case, the number of data values is doubled and then halved by the cyclic extension 4 and cyclic contraction 10 14 respectively.

In both cases, the exponential roll-off window 13 in the receiver are preferably the complex conjugate of the exponential roll-off window 5 in the transmitter.

The embodiments described above modulate the subcarriers with representations of the input data that are respectively equal positive and negative values of each input data. However, it is possible and in some cases desirable (such, as in the 15 presence of strong multipath interference) to use higher order schemes which use a greater number of representations of the input data.

By extension of the transmitter and receiver shown in Figs. 4 and 6 respectively, cubic cancellation can be achieved by using with the following transmitter 20 weighting and receiver weighting coefficients:

$$p_0 = 1, p_1 = -2, p_2 = 1$$

$$q_0 = 1, q_1 = -2, q_2 = 1$$

This corresponds with the polynomial:

$$1 - 2x - x^2$$

Fig. 16 is a scatterplot of symbols received for an embodiment that uses 64 subcarriers and cubic cancellation.

Fig. 17 is a graph showing the signal to ICI noise ratio of an embodiment of the invention compared with the signal to ICI noise ratio of a conventional OFDM
5 system.

Fig. 18 includes two graphs - an upper graph showing the power spectrum roll-off of a conventional OFDM system, and a lower graph showing the power spectrum roll-off of a typical embodiment.

OFDM systems can use various different schemes to modulate subcarriers, such
10 as phase shift keying (PSK) or quadrature amplitude modulation (QAM). Embodiments of the invention do not depend on the mapping of data to be transmitted to input data ($d_{0,i} \dots d_{D-1,i}$) and are therefore applicable to forms of modulation that can be used with OFDM generally.

Preferably a Fourier-based frequency transform, such as a DFT, or a discrete
15 cosine or sine transform (DCT or DST) is used in the described embodiments. However, it is not necessary that an orthogonal transform be of this type as there are a number of other orthogonal transforms that may also be suitable, such as the Walsh transform, the Hadamard transform and the various types of wavelet transforms.

20 The orthogonal transform can in certain embodiments make use of fact that data which modulates particular subcarriers is correlated, and similarly in the receiver it is the weighted and summed outputs that are important. Consequently, the computational complexity involved in transformation calculations can be significantly reduced by the use of appropriate algorithms which assume that
25 certain data points are correlated.

This involves appropriate exploitation of techniques for reducing the complexity of Fast Fourier Transform (FFT) calculations, for example, the decimation in time and decimation in frequency algorithms.

THE CLAIMS DEFINING THE INVENTION ARE AS FOLLOWS

- 1 A method of transmitting data in a multicarrier modulation system in which transform pairs allow communication using multiple subcarriers, the method including:
- 5 modulating representations of data on groups of subcarriers; and
- introducing a predetermined amount of intersymbol interference between symbols;
- wherein the modulation includes a modulation operation in which the data is effectively multiplied with weighting factors, before inverse transformation.
- 10
- 2 A method as claimed in claim 1, wherein the modulation includes a weighting operation in which the data is multiplied with weighting factors, before inverse transformation.
- 3 A method as claimed in claim 1, wherein the modulation includes a windowing operation in which the data is multiplied with a complex window, after inverse transformation.
- 15
- 4 A method as claimed in any one of claims 1 to 3, wherein the groups of subcarriers include non-overlapping sets of M adjacent subcarriers, and the M respective representations are integer multiples of the data, the integers corresponding with coefficients of the expanded polynomial expression $(1-x)^{M-1}$.
- 20
- 5 A method as claimed in any one of claims 1 to 4, wherein the data is modulated on a pair of adjacent subcarriers, and the representations of the data are multiples of 1 and -1.
- 25 6 A method as claimed in any one of claims 1 to 5, wherein introducing

intersymbol interference includes overlapping successive symbols to a predetermined extent by delaying and summing groups of samples of the symbols.

- 7 A method as claimed in claim 6, wherein successive symbols are
5 overlapped with each other by half a symbol period.
- 8 A method as claimed in any one of claims 1 to 7, wherein inverse
transformation includes using mathematical correlations between
representations of the data to reduce computational and/or memory
requirements of hardware on which the inverse transformation is
10 determined.
- 9 A method as claimed in claim 8, wherein said inverse transformation is
performed at least in part by a complex windowing operation.
- 10 A method as claimed in any one of claims 1 to 9, wherein subcarriers are
modulated by a summation of representations of different data.
- 15 11 A method as claimed in claim 10, wherein each subcarrier is modulated by
the difference between adjacent data.
- 12 A method as claimed in any one of claims 1 to 11, further including
providing pilot tones on subcarriers.
- 13 A method as claimed in claim 12, wherein relative values of the pilot tones
20 on successive symbols follows the sequence +1, 0, +1, 0, -1, 0, -1, 0.
- 14 A method of receiving data in a multicarrier modulation system in which
transform pairs allow communication using multiple subcarriers, the method
including:

demodulating data from representations of data on groups of

subcarriers; and

removing a predetermined amount of intersymbol interference between symbols;

5 wherein the demodulation includes a demodulation operation in which the representations are effectively multiplied with weighting factors, and the results summed after or, as part of transformation.

15 A method as claimed in claim 14, wherein the demodulation includes a weighting and summing operation in which the representations are multiplied with weighting factors, and the results summed after or, as part of
10 transformation.

16 A method as claimed in claim 14, wherein the demodulation includes a complex windowing operation in which the representations are multiplied with a complex window, before transformation.

17 A method as claimed in any one of claims 14 to 16, wherein the groups of
15 subcarriers include non-overlapping sets of M adjacent subcarriers, and the M respective representations are integer multiples of the data, the integers corresponding with coefficients of the expanded polynomial expression $(1-x)^{M-1}$.

18 A method as claimed in any one of claims 14 to 17, wherein the data is
20 effectively modulated on a pair of adjacent subcarriers, and the representations of the data are multiples of 1 and -1.

19 A method as claimed in any one of claims 14 to 18, wherein removing
intersymbol interference between symbols includes removing a
predetermined amount of intersymbol interference caused by overlapping
25 symbols to a predetermined extent.

- 20 A method as claimed in claim 19, wherein the predetermined amount of intersymbol interference is caused by overlapping symbols by half a symbol period.
- 21 A method as claimed in any one of claims 14 to 20, wherein removing intersymbol interference between symbols includes delaying groups of samples so that each transformation operates on samples which reduce the error rate.
- 22 A method as claimed in any one of claims 14 to 21, wherein removing intersymbol interference between symbols includes frequency domain equalisation.
- 23 A method as claimed in claim 22, wherein the frequency domain equalisation involves relatively few significant terms owing to the use of groups of subcarriers modulated by representations of the data.
- 24 A method as claimed in claim 21, wherein removing intersymbol interference between symbols includes frequency domain equalisation in which the form of calculations involved are the same for each subcarrier.
- 25 A method as claimed in any one of claims 21 to 24, wherein frequency domain equalisation operates on the output of the demodulation.
- 26 A method as claimed in any one of claims 14 to 25, wherein removing intersymbol interference includes a fixed operation for removing intersymbol interference caused by introduction of a predetermined amount of intersymbol interference, and an adaptive operation for removing intersymbol interference caused by reasons other than introduction of a predetermined amount of intersymbol interference.
- 27 A method as claimed in any one of claims 14 to 26, wherein transformation involves using mathematical correlations between representations of the

data to reduce computational and/or memory requirements of hardware on which the transformation is determined.

- 28 A method as claimed in claim 27, wherein said transformation is performed at least in part by a complex windowing removing operation.
- 5 29 A method as claimed in any one of claims 14 to 28, further including symbol synchronisation involving measuring the correlation between sections of signal, in which pilot tones are provided on subcarriers.
- 30 A method as claimed in claim 29, wherein relative values of the pilot tones on successive symbols follows the sequence +1, 0, +1, 0, -1, 0, -1, 0.
- 10 31 A method as claimed in any one of claims 14 to 30, further including frequency synchronisation involving measuring phase changes between the pilot tones provided on subcarriers.
- 32 A method as claimed in any one of claims 14 to 30, further including frequency synchronisation involving calculating a metric having a known
15 dependence on frequency offset.
- 33 A method as claimed in claim 32, wherein the metric approximates the multiplicative product of frequency offset and symbol period, and is calculated using the expression:

$$\operatorname{Re}\left(\frac{y_{k,i} + y_{k+1,i}}{y_{k,i} - y_{k+1,i}}\right)$$

- 20 34 A transmitter suitable for transmitting data in a multicarrier modulation system in which transform pairs allow communication using multiple subcarriers, the transmitter including:

means for modulating representations of data on groups of

subcarriers; and

means for introducing a predetermined amount of intersymbol interference between symbols;

5 wherein the modulation includes a modulation operation in which the data is effectively multiplied with weighting factors, before inverse transformation.

35 A transmitter as claimed in claim 34, wherein the modulation includes a weighting operation in which the data is multiplied with weighting factors, before inverse transformation.

10 36 A transmitter as claimed in claim 34, wherein the modulation includes a complex windowing operation in which the data is multiplied with a complex window, after inverse transformation.

37 A receiver suitable for receiving data in a multicarrier modulation system in which transform pairs allow communication using multiple subcarriers, the
15 receiver including:

means for demodulating data from representations of data on groups of subcarriers; and

means for removing a predetermined amount of intersymbol interference between symbols;

20 wherein the demodulation includes a demodulation operation in which the representations are effectively multiplied with weighting factors, and the results summed, after or as part of transformation.

38 A receiver as claimed in claim 37, wherein the demodulation includes a weighting and summing operation in which the representations are

*2nd
6th
10th*

multiplied with weighting factors, and the results summed, after or as part of transformation.

- 39 A receiver as claimed in claim 37, wherein the demodulation includes a
complex windowing operation in which the representations are multiplied
5 with a complex window, before transformation.
- 40 A multicarrier modulation system incorporating one or more transmitters as
claimed in any one of claims 34 to 36 and one or more receivers as claimed
in any one of claims 37 to 39, wherein the transmitters and receivers are
adapted to communicate with each other.
- 10 41 A multicarrier modulation system as claimed in claim 40, wherein the
weighting factors respectively used in the transmitter and the receiver have
equal relative values, or the complex windows respectively used in the
transmitter and the receiver are the complex conjugate of each other..

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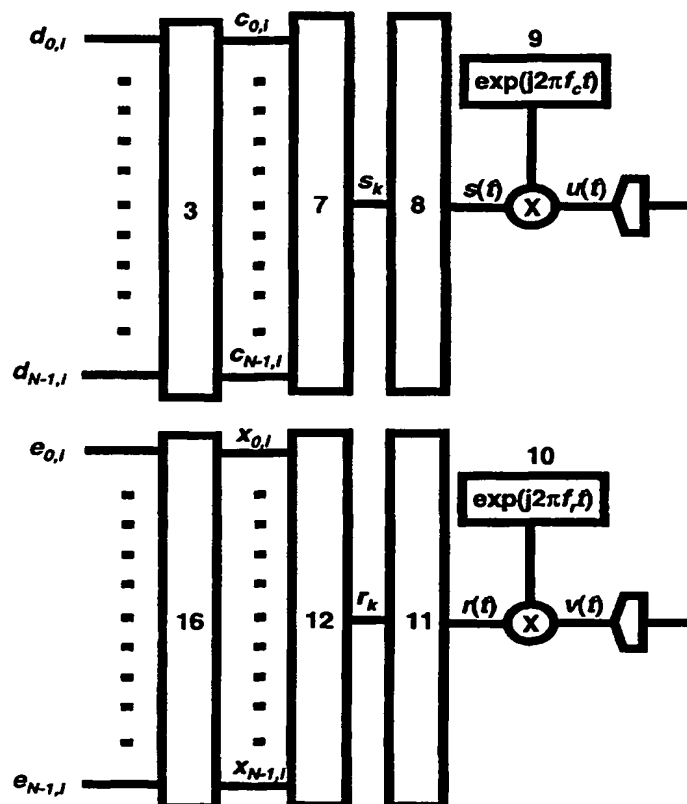
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(71)(72) Applicant and Inventor: ARMSTRONG, Jean [AU/AU]; 44 Longview Road, North Balwyn, VIC 3104 (AU).			
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(54) Title: DATA TRANSMISSION AND RECEPTION IN MULTICARRIER MODULATION SYSTEMS

(57) Abstract

The invention relates to methods and systems of transmitting and receiving data in multicarrier modulation systems, in which representations of input data are modulated on groups of subcarriers, and predetermined amounts of intersymbol interference are introduced between symbols. In the transmitter, adjacent subcarriers are respectively modulated with a positive and negative representation of an input data, and adjacent symbols are overlapped by half a symbol period. In the receiver, representations of the transmitted data are demodulated from the subcarriers, and the intersymbol interference removed so that the input data can be estimated. This provides particular advantages over conventional OFDM systems, while ensuring relatively high bandwidth efficiency.



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BE	Belgium	GN	Guinea	MK	The former Yugoslav Republic of Macedonia	TM	Turkmenistan
BF	Burkina Faso	GR	Greece			TR	Turkey
BG	Bulgaria	HU	Hungary	ML	Mali	TT	Trinidad and Tobago
BJ	Benin	IE	Ireland	MN	Mongolia	UA	Ukraine
BR	Brazil	IL	Israel	MR	Mauritania	UG	Uganda
BY	Belarus	IS	Iceland	MW	Malawi	US	United States of America
CA	Canada	IT	Italy	MX	Mexico	UZ	Uzbekistan
CF	Central African Republic	JP	Japan	NE	Niger	VN	Viet Nam
CG	Congo	KE	Kenya	NL	Netherlands	YU	Yugoslavia
CH	Switzerland	KG	Kyrgyzstan	NO	Norway	ZW	Zimbabwe
CI	Côte d'Ivoire	KP	Democratic People's Republic of Korea	NZ	New Zealand		
CM	Cameroon		Republic of Korea	PL	Poland		
CN	China	KR	Republic of Korea	PT	Portugal		
CU	Cuba	KZ	Kazakstan	RO	Romania		
CZ	Czech Republic	LC	Saint Lucia	RU	Russian Federation		
DE	Germany	LI	Liechtenstein	SD	Sudan		
DK	Denmark	LK	Sri Lanka	SE	Sweden		
EE	Estonia	LR	Liberia	SG	Singapore		

DATA TRANSMISSION AND RECEPTION IN MULTICARRIER MODULATION SYSTEMS

Field of the invention

The invention relates to data transmission and reception in multicarrier modulation
5 systems which use orthogonal transform pairs to allow communication on multiple subcarriers.

Background of the invention

Multicarrier modulation systems operate by dividing a serial data stream into
several parallel component data streams, and transmitting each of these parallel
10 data streams on separate subcarriers. At the receiving end, each of the parallel data streams is received, and arranged into a serial data stream corresponding with the serial data stream provided to the transmitter. Accordingly, in this type of system, only a small proportion of the total data is carried on each subcarrier.

While the power spectrum of each of the parallel data streams overlaps,
15 communication is possible as the subcarriers are generally orthogonal with each other over a symbol period. This is a direct consequence of the use of orthogonal transforms in the transmitter and receiver respectively. Using an N -point transform (and thus providing N subcarriers) effectively increases the symbol period by a factor of N .

20 There are various design issues which limit the practical application of multicarrier modulation systems.

Multicarrier modulation systems are generally sensitive to multipath effects, and are particularly sensitive to differences in the frequency of the local oscillators at the transmitter and receiver. Multicarrier modulation systems are also sensitive to
25 Doppler effects which are unavoidable in mobile and satellite applications.

Furthermore, multicarrier modulation systems suffer a lack of bandwidth

- containment, as the power spectrum roll-off is of the form $1/(f^2 N)$ where f is the frequency and N is number of subcarriers. The roll-off characteristics can be improved by increasing the number of subcarriers N , but this does not change the form of the roll-off. This gradual roll-off means that multicarrier modulation signals
- 5 must be sufficiently spaced in the frequency domain from other signals to avoid interference. However, this is unsatisfactory as it (a) does not alter the form of the power roll-off, (b) increases intercarrier interference due to increased sensitivity to frequency offsets. and (c) increases the computational complexity associated with the orthogonal transform.
- 10 Zhao and Häggman suggest using two representations of the input data (one the negative of the other) in order to reduce intercarrier interference ("Sensitivity to Doppler Shift and Carrier Frequency Errors in OFDM Systems - The Consequences and Solutions" *IEEE 46th Vehicular Technology Conference*, Atlanta, April 1996, pp. 1563-1568). However, this technique is not bandwidth
- 15 efficient.

It is an object of the invention to alleviate at least in part one or more of the problems of the prior art. More particularly, embodiments of the invention attempt to provide a multicarrier modulation communication system which improves out-of-band power leakage, and the effect of intercarrier and intersymbol interference,

20 while maintaining or increasing bandwidth efficiency.

Summary of the invention

The invention provides a method of transmitting data in a multicarrier modulation system in which transform pairs allow communication using multiple subcarriers, the method including:

5 modulating representations of data on groups of subcarriers; and

 introducing a predetermined amount of intersymbol interference between symbols.

The invention also provides a method of receiving data in a multicarrier modulation system in which transform pairs allow communication using multiple
10 subcarriers, the method including:

 demodulating data from representations of data on groups of subcarriers;
and

 removing a predetermined amount of intersymbol interference between symbols.

15 Furthermore, the invention correspondingly provides a transmitter and a receiver respectively including means capable of performing the inventive methods of transmitting and receiving data, as described above. The invention also provides a multicarrier modulation system including one or more such transmitters and one or more such receivers.

20 Preferably, introducing a predetermined amount of intersymbol interference is provided by overlapping symbols in the time domain. Preferably, this is achieved by selectively delaying and summing adjacent groups of symbols.

Modulation of subcarriers can be achieved using weighting techniques or alternatively windowing techniques.

Embodiments of the invention are applicable to multicarrier modulation systems that use any suitable scheme to modulate subcarriers. For example, phase-shift keying or quadrature amplitude modulation can be used. In principle, embodiments can use modulation schemes that are suitable for multicarrier modulation systems generally.

Embodiments of the invention are applicable to input data having an arbitrary statistical distribution. For instance, the input data may be previously coded using an error correcting code, by source coding or by any other relevant coding scheme, for example, code division multiple access (CDMA).

Embodiments of the invention are suitable for terrestrial as well as wireless systems. Various applications of particular embodiments include: (a) digital transmission over the public telephone network (for example, asymmetric digital subscriber loop (ADSL) and high-rate digital subscriber line (HDSL)) (b) digital audio broadcasting (c) digital mobile telephony (d) digital television broadcasting (e) satellite communications (f) wireless local area networks. Other applications, such as in relation to high bandwidth data storage technologies are also possible. While embodiments of the invention are described in relation to carrier systems, the principles of the invention are also applicable to baseband systems.

Embodiments of the invention are described in relation to orthogonal frequency division multiplexing (OFDM) systems, which are a particularly popular type of multicarrier system in which discrete Fourier transforms are used to provide subcarriers which are equally spaced in the frequency domain.

Description of drawings

Fig. 1 is a schematic diagram of a known OFDM system.

Fig. 2 is a graph representing the power roll-off of a typical prior art OFDM system. The x-axis is in frequency and the y-axis is in decibels (dB).

- 5 Fig. 3 is a graph representing the complex interference coefficients demonstrating the interference characteristics of a typical prior art OFDM system in the presence of typical values of carrier frequency offset. In this example $\Delta fT = 0.2$ and $N = 16$, with phase-offset equal to zero at the beginning of the symbol period. The real components of the complex interference coefficients are represented by diamonds and the imaginary components are represented by triangles.
- 10

Fig. 4 is a schematic diagram of a transmitter in accordance with an embodiment of the invention.

Fig. 5 is a schematic diagram of part of the transmitter shown in Fig. 4.

- Fig. 6 is a schematic diagram of a receiver in accordance with an embodiment of the invention.
- 15

Fig. 7 is a schematic diagram of the delay means of the receiver shown in Fig. 6.

Figs. 8 and 9 are schematic diagrams of parts of an estimation means of the receiver shown in Fig. 6.

- Fig. 10 is a schematic diagram of a transmitter and receiver which use a windowing technique to modulate and demodulate representations of input data to and from subcarriers.
- 20

Fig. 11 is a schematic diagram of a transmitter and receiver which use an alternative windowing technique to modulate and demodulate representations of input data to and from subcarriers.

Fig. 12 is a schematic diagram of a transmitter which uses three representations of input data to modulate subcarriers.

Fig. 13 is a schematic diagram of a transmitter which uses a general mapping of subcarriers to modulate subcarriers.

- 5 Figs. 14 to 16 are scatterplots representing symbols received for OFDM systems having 64 subcarriers using respectively no cancellation (conventional system), linear cancellation and cubic cancellation.

Fig. 17 is a graph representing the signal to intercarrier interference (ICI) noise ratio of an embodiment of the invention compared with the signal to ICI noise ratio of a conventional OFDM system. The y-axis is in decibels (dB) and the x-axis is in frequency offset as a proportion of the spacing between subcarriers. The upper curve is representative of a performance curve for an embodiment of the invention that provides cubic cancellation. The lower curve is representative of a performance curve for a conventional OFDM system.

- 15 Fig. 18 includes an upper graph representing the power spectrum roll-off of a conventional OFDM system, and a lower graph representing the power spectrum roll-off of an embodiment of the present invention. In both graphs the x-axis is in frequency and the y-axis is in decibels (dB).

Guide to terms and symbols

- 20 The following notation is used throughout the description in relation to various equations.

T	symbol period of symbol on input data channels
N	size of an orthogonal transform
P	number of weighted input data
25 D	number of input data in symbol period
W	number of weighting coefficients for each input data
$d_{0,i} \dots d_{D-1,i}$	input data of i -th symbol at input to weighting means

	$K_0 \dots K_{D-1}$	transmitter pre-weighting coefficients
	$p_0 \dots p_{W-1}$	transmitter weighting coefficients
	$g_1 \dots g_{W-1}$	transmitter generating polynomial coefficients
	$a_{0,i} \dots a_{N-1,i}$	weighted input data of i -th symbol, at output of weighting means and
5		input to orthogonal transform
	$c_{0,j} \dots c_{N-1,j}$	transmitter transform output data at output of orthogonal transform
	$N-m$	number of samples by which overlapping symbols are overlapped in the time domain
	s_k	transmitter aggregate data at output of parallel-to-serial converter
10		and input to digital-to-analog converter
	$s(t)$	transmitter baseband signal
	$u(t)$	analog transmission signal
	f_c	transmitter local oscillator frequency
	$\exp(j2\pi f_c t)$	transmitter local carrier signal
15	f_r	receiver local oscillator frequency
	$\exp(j2\pi f_r t)$	receiver local carrier signal
	Δf	local oscillator frequency difference
	$v(t)$	analog reception signal
	$r(t)$	receiver baseband signal
20	r_k	receiver aggregate data at output of analog-to-digital converter
	$x_{0,j} \dots x_{N-1,j}$	receiver transform input data of i -th symbol input to orthogonal transform
	$y_{0,i} \dots y_{N-1,i}$	receiver transform output data of i -th symbol at output of orthogonal transform
25	$v_{0,i} \dots v_{D-1,i}$	receiver demodulator data of i -th symbol at output of weighting means
	$q_0 \dots q_{W-1}$	receiver weighting coefficients
	$e_{0,i} \dots e_{D-1,i}$	output data of i -th symbol at output of estimator
	$C_0 \dots C_{N-1}$	complex interference coefficients

30

Description of embodiments

Fig. 1 shows a known OFDM system. This type of transmission system was developed in order to provide a high-data bandwidth efficient system for data transmission. The basic principle is to allow the spectra of the subchannels of the data transmission system to overlap in order to make better use of the available bandwidth. Overlapping subcarrier spectra is possible as the signal carried by each subcarrier is mathematically orthogonal to each other over a symbol period as a result of the use of an orthogonal transform 3 such as a discrete Fourier transform (DFT).

In reference to Fig. 1, input data $d_{0,i} \dots d_{N-1,i}$ to be transmitted is directly input to an orthogonal transform 3, the output of which is transmitter transform output data $c_{0,i} \dots c_{N-1,i}$ that is input directly to a parallel-to-serial converter 7. The parallel-to-serial converter 7 produces transmitter aggregate data s_k that is a linear sequence of values appropriate for transmission. The parallel-to-serial converter 7 produces transmitter aggregate data s_k on a transmitter aggregate data channel.

The serial output is termed transmitter aggregate data s_k that is then input to a digital-to-analog converter (DAC) 8. The output from the DAC 8 is then a transmitter baseband signal $s(t)$.

This transmission channel can be any appropriate channel, and the characteristics of the analog transmission signal $u(t)$ are chosen to accommodate the transmission channel.

The receiver receives the analog transmission signal $u(t)$ as an analog reception signal $v(t)$, and in this sense the analog reception signal $v(t)$ corresponds with the analog transmission signal $u(t)$. Of course, in the prior art systems as in embodiments of the invention, these signals are not identical except in an ideal, noiseless transmission channel. In real systems, the analog reception signal $v(t)$ is a noisy, distorted representation of the analog transmission signal $u(t)$.

The receiver receives the analog reception signal $v(t)$ and multiplies it by a receiver local carrier signal $\exp(j2\pi f_c t)$ to obtain a receiver baseband signal $r(t)$. This receiver baseband signal $r(t)$ is input to an analog-to-digital converter (ADC)

11. The output of the ADC 11 provides receiver aggregate data r_k is input to a serial-to-parallel converter 12 that provides receiver transform input data $x_{0,i} \dots x_{N-1,i}$ to an orthogonal transform 16. The orthogonal transform 16 then provides output data $e_{0,i} \dots e_{N-1,i}$ that corresponds with the input data $d_{0,i} \dots d_{N-1,i}$.

- 5 In the prior art as in embodiments of the invention, the orthogonal transforms 3 and 16 in the transmitter and receiver respectively, are the inverse of each other. Conceptually, it is considered that the orthogonal transform 3 in the transmitter is an inverse transform to provide a mapping from the frequency domain to the time domain and the orthogonal transform 16 in the receiver is a forward transform to
10 provide a mapping from the time domain back to the frequency domain.

In an ideal system, the output data $e_{0,i} \dots e_{N-1,i}$ is precisely equal to the input data $d_{0,i} \dots d_{N-1,i}$. However, as previously outlined, this is not the case in practical systems as are known in the prior art.

- In an OFDM receiver, the analog reception signal $v(t)$ is translated down to
15 baseband to produce the receiver baseband signal $r(t)$. If the other carriers all beat down to frequencies that, in the time domain, have a whole number of cycles in the symbol period (T), there is zero contribution from all these other subcarriers. Thus the subcarriers are mathematically orthogonal if the subcarrier spacing is a multiple of $1/T$. This condition is a natural result of using an orthogonal transform
20 pair 3 and 16 such as a IDFT and DFT in the transmitter and receiver respectively.

Known OFDM systems such as that described above, are deficient as earlier outlined. Fig. 2 demonstrates the power spectra of an OFDM signal which demonstrates the lack of bandwidth containment of the known OFDM system shown in Fig. 1.

- 25 Fig. 3 is a graph of complex interference coefficients ($C_0 \dots C_{N-1}$) for illustrative values of frequency offset ($\Delta f T = 0.2$ and $N = 16$, with phase-offset equal to zero at the beginning of the symbol period). Frequency offset Δf can arise due to absolute differences in the frequencies f_c and f_r of local oscillators in the transmitter and receiver respectively, and by Doppler shifts due to relative motion

of transmitter and receiver. Frequency offset results in ICI, which is quantitatively indicated by complex interference factors.

In Fig. 3, real components of the complex interference coefficients are represented by diamonds and the imaginary components are represented by triangles. ICI may be interpreted in terms of the complex interference coefficients ($C_0 \dots C_{N-1}$) that measure the contribution of a transmitter subcarrier to each demodulated subcarrier; that is, the interference in one subcarrier arising from effects between subcarriers.

As can be seen from Fig. 3, the complex interference coefficients ($C_0 \dots C_{N-1}$) vary smoothly between subcarriers except at the transitions from the reference subcarrier (whose impact on other subcarriers is being measured) to its immediately adjacent subcarriers.

It is observed that the form of variation of complex interference coefficients ($C_0 \dots C_{N-1}$) across subcarriers can be closely modelled by a relatively low order polynomial equation. This predicability allows for generally consistent cancellation of ICI by modulating groups of subcarriers with representations of the data.

An example embodiment of the invention is now described in relation to Fig. 4 and Fig. 5.

Fig. 4 shows a transmitter in accordance with an embodiment of the invention. Compared with the OFDM system shown in Fig. 1, the transmitter shown in Fig. 4 provides for modulating representations of data on groups of subcarriers, and introducing a substantially predetermined amount of intersymbol interference between symbols.

The input data ($d_{0,i} \dots d_{D-1,i}$) is provided on input data channels. Representations of the input data are modulated onto groups of subcarriers by multiplying each input data through a weighting means 1 to provide weighted input data which is then input to an orthogonal transform 3. In Fig. 4, the weighting means 1 includes what are represented as a collection of the transmitter weighting coefficients (p_0 and

p_1). Each input data ($d_{0,i} \dots d_{D-1,i}$) on the input data channels is multiplied by transmitter weighting coefficients (p_0 and p_1) in order to generate two weighted representations of each of the input data ($d_{0,i} \dots d_{D-1,i}$). Collectively these weighted representations of the input data ($d_{0,i} \dots d_{D-1,i}$) are the weighted input data ($a_{0,i} \dots a_{N-1,i}$) which are used to modulate two adjacent subcarriers. It is not necessary that every subcarrier be used. (For example, in baseband applications, it is necessary that the input to the transform have Hermitian symmetry so that the output has no imaginary components.) Rather, every subcarrier should be paired with an oppositely weighted subcarrier. Preferably, paired subcarriers are adjacent to each other.

The orthogonal transform 3 has N inputs that directly correspond with the number of subcarriers N modulated by representations of the input data, in this case the weighted input data. Each output of the orthogonal transform 3 in the transmitter corresponds with a transmitter transform output data channel.

Fig. 5 shows the interaction of a delay means 6 and the parallel-to-serial converter 7. Half of the transmitter transform output data from the orthogonal transform 3 is passed to a delay means 6 which together with parallel-to-serial converter 7 and the addition operation introduces a known and predetermined amount of intersymbol interference between symbols. The first $N/2$ elements of the transmitter transform output data are converted to serial form, while the second $N/2$ elements are first delayed by $T/2$ before parallel-to-serial conversion. Each delayed output data is summed with a non delayed output, so that each transmitter aggregate data is the summation of two samples from adjacent symbols.

Accordingly, each transmitter aggregate data is the summation of two terms from adjacent symbols. The table below shows the relationship between the aggregate data and the transmitter transform output data for an overlap of $T/2$.

$C_{4,i-1}$	$C_{5,i-1}$	$C_{6,i-1}$	$C_{7,i-1}$								
$C_{0,i}$	$C_{1,i}$	$C_{2,i}$	$C_{3,i}$	$C_{4,i}$	$C_{5,i}$	$C_{6,i}$	$C_{7,i}$				
				$C_{0,i+1}$	$C_{1,i+1}$	$C_{2,i+1}$	$C_{3,i+1}$	$C_{4,i+1}$	$C_{5,i+1}$	$C_{6,i+1}$	$C_{7,i+1}$
								$C_{0,i+2}$	$C_{1,i+2}$	$C_{2,i+2}$	$C_{3,i+2}$
S_k	S_{k+1}	S_{k+2}	S_{k+3}	S_{k+4}	S_{k+5}	S_{k+6}	S_{k+7}	S_{k+8}	S_{k+9}	S_{k+10}	S_{k+11}

In this example, N is 8 for simplicity. Considering the i -th transform output data, the first N/2 elements are added term by term to the last N/2 elements of the $(i-1)$ th transmitter transform output data, for example, $C_{0,i}$ is added to $C_{N/2,i-1}$, $C_{1,i}$ is added to $C_{N/2+1,i-1}$ and so on. Similarly the last N/2 elements are added term by term to the first N/2 elements of the $(i+1)$ th transmitter transform output data.

There are three operations involved in converting the transmitter transform output data to the aggregate data. These are delaying, adding and parallel-to-serial conversion. Of course, these operations need not necessarily be this order. The delaying and adding operations can either occur before or after the parallel-to-serial conversion. Alternatively, delaying can occur before parallel-to-serial conversion, with adding occurring after parallel-to-serial conversion.

In the embodiment shown in Fig. 4, and its delay means 6 shown in Fig. 5, successive symbol interferes with each other by half a symbol period. However, there are other ways in which intersymbol interference can be introduced in this way. For example, it is possible to use a general overlap of $N-m$ samples between adjacent symbols. A new symbol begins transmission every mT/N seconds. Thus, if more than two symbols overlap, each transmitter aggregate data correspondingly involves a summation including more terms. If $m = N/4$, then four symbols are added, and four values summed. A similar delay means 6 and parallel-to-serial converter 7 as shown in Fig. 5 can be used, with modifications as appropriate.

Introducing intersymbol interference by overlapping adjacent symbols has the advantage of improving the distribution of instantaneous signal amplitudes in the transmitted signal. Using an overlap of $T/2$ results in a constant amplitude

envelope. Progressively increasing the amount of intersymbol interference increases the data rate, but also increases the complexity of the receiver, and increases the effect of added noise in the transmission channel.

The transmitter aggregate data s_k produced by the parallel-to-serial converter 7 is passed through a digital-to-analog converter 8 to produce a transmitter baseband signal $s(t)$.

Fig. 6 shows a receiver corresponding with the transmitter shown in Fig. 4. Two operations are required: demodulating the groups of subcarriers and removing the intersymbol interference. Delay means 15 in combination with orthogonal transform 16 and weighting means 17 can be considered to provide demodulation, while storage means 18 and equaliser 19 can be considered to remove intersymbol interference.

In Fig. 6, the receiver aggregate data r_k is input to a delay means 15 that outputs receiver transform input data ($x_{0,i} \dots x_{N-1}$). The delay means 15 is used to provide the orthogonal transform 16 with different combinations of receiver delay data so that the output data can be subsequently weighted and added using weighting means 17 as described below. The weighting means 17 weights and sums the receiver transform output data. The coefficients q_0, q_1 used in the weighting means 17 are preferably the same as p_0, p_1 as discussed below.

Fig. 7 shows the delay means 15 in Fig. 6 in more detail. The delay means 15 is designed to achieve symbol synchronisation with the aim of reducing error rate after equalisation. An N-stage shift register 15B is used to hold the data delayed by delay means 15A so that the receiver transform input data presented to the orthogonal transform 16 represents N successive values of the receiver delay data. The data is then shifted N/2 stages up the shift register before the next orthogonal transform is performed.

r_k	r_{k+1}	r_{k+2}	r_{k+3}	r_{k+4}	r_{k+5}	r_{k+6}	r_{k+7}	r_{k+8}	r_{k+9}	r_{k+10}	r_{k+11}
$x_{4,i-1}$	$x_{5,i-1}$	$x_{6,i-1}$	$x_{7,i-1}$								
$x_{0,i}$	$x_{1,i}$	$x_{2,i}$	$x_{3,i}$	$x_{4,i}$	$x_{5,i}$	$x_{6,i}$	$x_{7,i}$				

$x_{0,i+1}$	$x_{1,i+1}$	$x_{2,i+1}$	$x_{3,i+1}$	$x_{4,i+1}$	$x_{5,i+1}$	$x_{6,i+1}$	$x_{7,i+1}$
				$x_{0,i+2}$	$x_{1,i+2}$	$x_{2,i+2}$	$x_{3,i+2}$

For example, consider the case of $N=8$ as shown in the above table. The delay means 15 operates to output the receiver aggregate data $r_k \dots r_{k+7}$, as the receiver transform input data $x_{0,i} \dots x_{7,i}$. The transform input data are the values that transform 16 uses for the i -th transform operation. Once this has occurred, $r_{k+4} \dots r_{k+7}$ are shifted up the register and values $r_{k+8} \dots r_{k+11}$ are shifted in. The $(i+1)$ -th transform operation is then performed using output receiver aggregate data $r_{k+4} \dots r_{k+11}$, as the receiver transform input data $x_{0,i+1} \dots x_{7,i+1}$. Thus receiver transform operations are performed at intervals $T/2$. For the case of perfect synchronisation and no distortion and no noise in the channel, $r_k = s_k$. This means that all of the values of r_k which depend on the transmitter transform output data $c_{0,i} \dots c_{N-1,i}$ which are the results of the i -th transmitter transform are used as input to the i -th receiver transform.

In practice distortion in the channel will mean that , $r_k \neq s_k$ and that more than N samples of the receiver aggregate data depend on $c_{0,i} \dots c_{N-1,i}$. In this case the symbol synchronisation circuits operate to minimise the error rate after equalisation.

Fig. 7 shows the symbol synchronisation being achieved by a variable delay. In practice, symbol synchronisation can also be achieved by varying the sampling instants of the ADC and/or by controlling the clocking of data into the shift register 15B.

Embodiments of the invention do not use cyclic prefixes to avoid intersymbol interference, and accordingly it is not possible to achieve symbol synchronisation or frequency synchronisation by using correlations between the cyclic prefix and the symbol. Instead, it is appropriate to use other methods which use pilot tones, or which are blind estimation techniques based on the properties of the modulation method.

A pilot tone approach can be used by using one or more subcarriers as pilot tones modulated by predetermined values. For an overlap of $T/2$, the correlation between adjacent sections of signal spaced $T/2$, T or higher multiples of $T/2$ apart can be measured either before or after the receiver transform 16. The symbol
5 timing is adjusted according to the estimated symbol timing error.

For an overlap of $T/2$, particularly simple algorithms can be used if the relative weightings of pilots in eight successive symbols are +1, 0, +1, 0, -1, 0, -1. These give an output which is a linear function of symbol timing error.

- 10 Pilot techniques also have the advantage that they can be used to estimate synchronization error for any initial timing error unlike cyclic prefix synchronisation techniques, which may be limited in their capture range by the length of the cyclic prefix used.

The number of pilots can be varied to achieve an appropriate compromise
15 between timing jitter and loss in bandwidth. More pilots can be used at the start of transmission to increase the initial timing acquisition.

In a similar way, frequency synchronization can be achieved by measuring the change in phase of pilot tones between symbols.

- Blind algorithms are another class of symbol synchronisation or frequency
20 synchronization techniques that use characteristics of the incoming signal to detect and correct synchronisation errors. For example, blind algorithms for frequency synchronisation can use techniques that depend on the effect of frequency offset in changing the relative amplitudes of subcarriers which have been modulated in a group. For the case of modulation onto pairs of subcarriers,
25 with no frequency error or distortion, the pair of subcarriers when demodulated have values which are the negative of each other. Frequency offset upsets this balance in a known way, and can thus be used as a basis for frequency synchronization. For example, consider the receiver shown in Fig. 6. In the

absence of frequency error or other distortion, $y_k = -y_{k+1}$ for even k . This balance is disturbed by frequency error. The metric shown directly below approximates ΔfT for large N .

$$\text{Re} \left(\frac{y_{k,i} + y_{k+1,i}}{y_{k,i} - y_{k+1,i}} \right)$$

- 5 This metric does not depend on the data used to modulate the subcarrier pair, and hence frequency synchronization can be achieved from the data without pilot tones.

Figs. 8 and 9 respectively show a storage means 18 and equaliser 19, which in combination estimate the transmitted data. The storage means 18 includes a
 10 number of storage elements 18A - 18E, each of which is regularly updated each $T/2$ so that it successively stores data $v_{0,i} \dots v_{N/2-1,i}$ for use by the equaliser 19. Each $T/2$, data from one element is passed to the next. The equaliser 19, which completes estimation of the representations of the data from the subcarriers. The equaliser 19 operates on a sequence of output vectors (in Fig. 9, $V_i = v_{0,i} \dots v_{N/2-1,i}$
 15 and $E_i = e_{0,i} \dots e_{N/2-1,i}$) from the storage means 18 to output the output data which estimates the input data provided to the transmitter.

The equaliser shown in Fig. 9 has seven vectors as input, and the storage means 18 has a corresponding number of elements. However, simpler implementations using less vectors V_i , may be sufficient. The number of input vectors needed
 20 depends on the degree of distortion in the channel, the amount of overlap and the signal to noise ratio.

In the example shown, a frequency domain equaliser is used in the receiver to recover the transmitted data. However, a time domain equaliser can alternatively be used. A time domain equaliser would operate before the orthogonal transform
 25 16, while the frequency domain equalizer operates after the orthogonal transform 16. Frequency domain equalisers are preferred as relatively simple and effective equalisers can be used as a consequence of the characteristics of modulating representations of data on groups of adjacent subcarriers.

All of the forms of equalization used in one dimensional applications can be adapted to this two-dimensional problem including linear equalization, decision feedback equalization and maximum likelihood sequence estimation (MLSE). When decision feedback equalization is used, error correcting coding across the data in one symbol can be used to reduce the probability of error propagation.

Thus an equaliser of relative simplicity compared with previously suggested equalisers can be used. There are various reasons for this. Firstly, the weighting and adding block at the input reduces the number of inputs to the equalizer. The modulation on groups of subcarriers results in an impulse response which has relatively few significant terms. As a result, simpler equalisers can be designed without significant loss in performance. Furthermore, for the particular case of an overlap of $T/2$, the form of the interference is independent of the index of the input. This means that for the case of no distortion (that is where the equaliser is only correcting for the overlap of symbols) the structure of the equaliser is symmetric in some respects, which provides an opportunity for relatively simple equaliser structure. Alternative embodiments can be used in which the equaliser has two stages, a fixed equaliser to correct for the deliberately introduced overlap, followed by a simpler adaptive equalizer which corrects for the channel.

The transmitter described above and shown in Fig. 4 uses weighting means 1 to modulate groups of subcarriers with representations of the input data. However, this can alternatively be done by using windowing-based techniques.

Fig. 10 shows a example of a transmitter and receiver which uses windowing methods to modulate subcarriers with representations of the input data. N point orthogonal transforms 3 and 16 having more inputs/outputs than are otherwise necessary are used in combination with exponential roll-off windows 5 and 13. That is, the inputs to the orthogonal transform 3 alternate between zero and input data. The complex exponential window 5 is of the form: $[1 - \exp(j2\pi \cdot l/N)]$.

Fig. 11 shows an alternative approach. $N/2$ point orthogonal transforms 3 and 16 are used in combination with a cyclic extension 4 and cyclic contraction 14, and exponential roll-off windows 5 and 13. The $N/2$ point orthogonal transform 3

provides a cyclic extension 4 of $N/2$ points. Again the complex window 5 is of the form $[1 - \exp(j2\pi \cdot l/M)]$.

In both cases, the complex window 5, of the form $[1 - \exp(j2\pi \cdot l/M)]$, acts to multiply the l -th value of the transmitter transform output data by a factor of $[1 - \exp(j2\pi \cdot l/M)]$ before further processing.

The cyclic contraction required in the receiver is preferably achieved by simply performing an element-by-element summation of the data points indexed $0 \dots N/2-1$ with those data points indexed $N/2 \dots N-1$. In this case, the number of data values is doubled and then halved by the cyclic extension 4 and cyclic contraction 10 14 respectively.

In both cases, the exponential roll-off window 13 in the receiver are preferably the complex conjugate the exponential roll-off window 5 in the transmitter.

The embodiments described above modulate the subcarriers with representations of the input data that are respectively equal positive and negative values of each input data. However, it is possible and in some cases desirable (such, as in the 15 presence of strong multipath interference) to use higher order schemes which use a greater number of representations of the input data.

By extension of the transmitter and receiver shown in Figs. 4 and 6 respectively, cubic cancellation can be achieved by using with the following transmitter 20 weighting and receiver weighting coefficients:

$$p_0 = 1, p_1 = -2, p_2 = 1$$

$$q_0 = 1, q_1 = -2, q_2 = 1$$

This corresponds with the polynomial:

$$1 - 2x - x^2$$

Similarly, quintic cancellation can be achieved with the following transmitter weighting coefficients and receiver weighting coefficients for $W = 4$.

$$p_0 = 1, p_1 = -3, p_2 = 3, p_3 = -1$$

$$q_0 = 1, q_1 = -3, q_2 = 3, q_3 = -1$$

5 This corresponds with the polynomial:

$$1 - 3x + 3x^2 - x^3$$

Still higher order schemes can be provided by generating further representations which are used to modulate a correspondingly greater number of subcarriers. Representations can be generated in accordance with the polynomial $(1-x)^{W-1}$. The
10 coefficients can be provided by expanding this polynomial.

Fig. 12 shows an embodiment which uses three representations of each input data to modulate a group of subcarriers. The weightings p_0, p_1, p_2 are complex coefficients of the polynomial $(1-x)^{W-1}$ where $W = 3$. The factors $K_0 \dots K_{D-1}$ are complex factors which scale the representations provided by weightings p_0, p_1, p_2 ,
15 allowing for relative changes in amplitude and phase between the values modulated on respective subcarriers.

The values of $K_0 \dots K_{D-1}$ can be made unity. However, in some cases, it is desirable to modify amplitude and phase by modifying $K_0 \dots K_{D-1}$. For example, it may be necessary to adjust the amplitude of certain channels to equalise the
20 signal. Similarly, it may be necessary to adjust the phase of the signal to modify its power characteristics.

If complex pre-weighting factors $K_0 \dots K_{D-1}$ in the transmitter, as shown Fig. 12, it is appropriate to also use corresponding post-weighting factors $L_0 \dots L_{D-1}$ in the receiver. For example, it may be appropriate to use post-weight factors $L_0 \dots L_{D-1}$
25 which are the inverse, or complex conjugate, of the pre-weighting factors $K_0 \dots K_{D-1}$ in the transmitter. Of course, pre-weighting and post-weighting factors can be

used in other cases, for example, when only two weight factors are used.

Fig. 13 shows a further embodiment of a transmitter having a generalised mapping between input data ($d_{0,i} \dots d_{D-1,i}$) and weighted input data ($a_{0,i} \dots a_{P-1,i}$). ICI cancellation is achieved in the transmitter so that the individual decoded weighted
 5 output data ($z_{0,i} \dots z_{P-1,i}$) in the receiver is relatively free of ICI and is used to estimate the input data ($d_{0,i} \dots d_{D-1,i}$).

Most simply, mapping of the input data ($d_{0,i} \dots d_{D-1,i}$) onto weighted input data ($a_{0,i} \dots a_{P-1,i}$) can be arranged so that there is a direct mapping from the x possible values that the input data d can take (typically this would be a power of 2, ie 2, 4,
 10 8, 16 etc) to x combinations chosen to fit some particular criterion. For example, the criterion could be maximum Euclidean distance to minimise error rate or some combination of limitation of power roll-off, insensitivity to frequency offset, minimise peak-to-mean power ratio. Any other criterion, or compromise between competing criteria could be chosen as appropriate for a given application.

15 As an example, consider the case of grouping in fours in the transmitter. There are various ways that this can be achieved.

To achieve linear cancellation with four carriers, the carriers must be weighted with the coefficients of

$$(1-x)^2(g_0+g_1x)$$

20 where g_0 and g_1 are any values including complex values. Different values of input data can be mapped to different combinations of g_0 and g_1 . For example, g_0 and g_1 could be allowed to take values $1+j$, $1-j$, $-1+j$, $-1-j$. Then there are sixteen possible combinations and 4 bits could be mapped onto the four carriers.

At the receiver z_0 is used as an estimate of g_0 and z_3 is used as an estimate of g_1 .
 25 The linear component of ICI is cancelled in each of these values. However, the performance with respect to noise is not optimal due to the asymmetry between transmitter and receiver, and the consequent breakdown of the matched filter

condition.

Alternatively, the mappings can be changed from symbol period to symbol period in a predetermined way to implement codes in some respects analogous to trellis code modulation. Preferably, $2x$ combinations could be defined, but only x would
5 be allowable in any particular symbol period.

As mentioned earlier, subcarriers can be multiplied by factors to adjust peak-to-mean power. Wilkinson and Jones ("Minimisation of the Peak to Mean envelope Power Ratio of Multicarrier Transmission Schemes by Block Coding", *IEEE 45th Vehicular Technology Conference*, Chicago, 1995, pp.825-829) discusses how
10 coding can be used to reduce peak-to-mean power in OFDM systems.

Of course, it is not necessary that each input data has the same number of representations. For example, it may be desirable to provide modulate a greater number of representations of input data on subcarriers near the frequency boundaries of the signal. This has the advantage of a steeper power spectrum roll-
15 off at the frequency domain boundaries of the signal. Similarly, it is not necessary to use all of the subcarriers. Some subcarriers can be left unmodulated, as may be preferred in some embodiments.

In alternative embodiments, it is possible to have each (or alternating) subcarriers modulated by values which are a summation of representations of different input
20 data. While this reduces the number of subcarriers for a given number of input data, it is generally not found to be advantageous and is accordingly not preferred.

Fig. 14 to Fig. 16 are performance graphs of particular embodiments compared with comparable conventional systems.

Fig. 14 is a scatterplot of symbols received for a typical prior art OFDM system
25 with 64 subcarriers.

Fig. 15 is a scatterplot of symbols received for an embodiment of the present invention that uses 64 subcarriers and linear cancellation.

Fig. 16 is a scatterplot of symbols received for an embodiment that uses 64 subcarriers and cubic cancellation.

Fig. 17 is a graph showing the signal to ICI noise ratio of an embodiment of the invention compared with the signal to ICI noise ratio of a conventional OFDM system.

Fig. 18 includes two graphs - an upper graph showing the power spectrum roll-off of a conventional OFDM system, and a lower graph showing the power spectrum roll-off of a typical embodiment.

OFDM systems can use various different schemes to modulate subcarriers, such as phase shift keying (PSK) or quadrature amplitude modulation (QAM). Embodiments of the invention do not depend on the mapping of data to be transmitted to input data $(d_{0,i} \dots d_{D-1,i})$ and are therefore applicable to forms of modulation that can be used with OFDM generally.

Preferably a Fourier-based frequency transform, such as a DFT, or a discrete cosine or sine transform (DCT or DST) is used in the described embodiments. However, it is not necessary that an orthogonal transform be of this type as there are a number of other orthogonal transforms that may also be suitable, such as the Walsh transform, the Hadamard transform and the various types of wavelet transforms.

The orthogonal transform can in certain embodiments make use of fact that data which modulates particular subcarriers is correlated, and similarly in the receiver it is the weighted and summed outputs that are important. Consequently, the computational complexity involved in transformation calculations can be significantly reduced by the use of appropriate algorithms which assume that certain data points are correlated.

This involves appropriate exploitation of techniques for reducing the complexity of Fast Fourier Transform (FFT) calculations, for example, the decimation in time and decimation in frequency algorithms.

To illustrate this point, the discrete Fourier algorithm is usually expressed as a linear summation of complex exponential terms:

$$X(k) = \sum_{n=0}^{N-1} x(n) W_N^{kn}$$

where

5
$$W_N = \exp(-j2\pi/N)$$

If $x(n)$ is an input sequence in which alternate terms are the negative of each other, then the expression above can be rearranged:

$$\begin{aligned} X(k) &= \sum_{\substack{n=0 \\ n \text{ even}}}^{N-1} x(n) W_N^{kn} - W_N^k \sum_{\substack{n=0 \\ n \text{ even}}}^{N-1} x(n) W_N^{kn} \\ &= (1 - W_N^k) \sum_{\substack{n=0 \\ n \text{ even}}}^{N-1} x(n) W_N^{kn} \end{aligned}$$

This allows an N point calculation to be reduced to an N/2 point calculation,
10 followed by multiplication by a constant factor.

Further to the above embodiments, there are a variety of systems that are not limited to a single transmitter and a single receiver. A number of transmitters may be provided to provide a broadcast coverage of a signal. Similarly, a number of receivers can be provided for multiple users. In such broadcast systems there are
15 also known to be systems whereby different transmitters and receivers may be assigned to different subsets of subcarriers. Some of these ideas are outlined in a recent paper by A.C. Caswell ("Multicarrier Transmission in a Mobile Radio Channel", *Electronic Letters*, 10th October 1996 Vol 32 pp. 1962-1963).

It will be understood that the invention disclosed and defined in this specification
20 extends to all alternative combinations of two or more of the individual features mentioned or evident from the text or drawings. All of these different combinations constitute various alternative aspects of the invention.

THE CLAIMS DEFINING THE INVENTION ARE AS FOLLOWS

1. A method of transmitting data in a multicarrier modulation system in which transform pairs allow communication using multiple subcarriers, the method including:
 - 5 modulating representations of data on groups of subcarriers; and
 - introducing a predetermined amount of intersymbol interference between symbols.
2. A method as claimed in claim 1 wherein the groups of subcarriers include non-overlapping sets of M adjacent subcarriers, and the M respective representations
10 are integer multiples of the data, the integers corresponding with coefficients of the expanded polynomial expression $(1-x)^{M-1}$.
3. A method as claimed in any one of claims 1 or 2 wherein the data is modulated on a pair of adjacent subcarriers, and the representations of the data are multiples of 1 and -1.
- 15 4. A method as claimed in any one of claims 1 to 3 wherein introducing intersymbol interference includes overlapping successive symbols to a predetermined extent by delaying and summing groups of samples of the symbols.
5. A method as claimed in claim 4 wherein successive symbols are overlapped with each other by half a symbol period.
- 20 6. A method as claimed in any one of claims 1 to 5 wherein the modulation includes a weighting operation in which the data is multiplied with weighting factors, before inverse transformation.
7. A method as claimed in any one of claims 1 to 5 wherein the modulation involves a windowing operation in which the data is multiplied with a window, after
25 inverse transformation.

8. A method as claimed in any one of claims 1 to 7 wherein inverse transformation includes using mathematical correlations between representations of the data to reduce computational and/or memory requirements of hardware on which the inverse transformation is determined.
- 5 9. A method as claimed in any one of claims 1 to 5 wherein subcarriers are modulated by a summation of representations of different data.
10. A method as claimed in claim 9 wherein each subcarrier is modulated by the difference between adjacent data.
11. A method as claimed in any one of claims 1 to 10 including providing pilot
10 tones on subcarriers.
12. A method as claimed in claim 11 wherein relative values of the pilot tones on successive symbols follows the sequence +1, 0, +1, 0, -1, 0, -1, 0.
13. A method of receiving data in a multicarrier modulation system in which transform pairs allow communication using multiple subcarriers, the method
15 including:
- demodulating data from representations of data on groups of subcarriers;
and
- removing a predetermined amount of intersymbol interference between symbols.
- 20 14. A method as claimed in claim 13 wherein the groups of subcarriers include non-overlapping sets of M adjacent subcarriers, and the M respective representations are integer multiples of the data, the integers corresponding with coefficients of the expanded polynomial expression $(1-x)^{M-1}$.
15. A method as claimed in any one of claims 13 or 14 wherein the data is
25 modulated on a pair of adjacent subcarriers, and the representations of the data

are multiples of 1 and -1.

16. A method as claimed in any one of claims 13 to 15 wherein the demodulation includes a weighting and summing operation in which the representations are multiplied with weighting factors, and the results summed, after transformation.

5 17. A method as claimed in any one of claims 13 to 15 wherein the demodulation includes a weighting and summing operation in which the representations are multiplied with weighting factors, and the results summed, as part of transformation.

10 18. A method as claimed in any one of claims 13 to 15 wherein the demodulation includes a windowing operation in which the representations are multiplied with a window, before transformation.

15 19. A method as claimed in any one of claims 13 to 18 wherein removing intersymbol interference between symbols includes removing a predetermined amount of intersymbol interference caused by overlapping symbols to a predetermined extent.

20. A method as claimed in claim 19 wherein the predetermined amount of intersymbol interference is caused by overlapping symbols by half a symbol period.

20 21. A method as claimed in any one of claims 13 to 20 wherein removing intersymbol interference between symbols includes delaying groups of samples so that each transformation operates on samples which reduce the error rate.

22. A method as claimed in any one of claims 13 to 20 wherein removing intersymbol interference between symbols includes frequency domain equalisation.

25 23. A method as claimed in claim 22 wherein frequency domain equalisation involves relatively few significant terms owing to the use of groups of subcarriers

modulated by representations of the data.

24. A method as claimed in claim 20 wherein removing intersymbol interference between symbols includes frequency domain equalisation in which the form of calculations involved are the same for each subcarrier.

5 25. A method as claimed in any one of claims 22 to 24 wherein frequency domain equalisation operates on the output of the demodulation.

26. A method as claimed in any one of claims 13 to 25 wherein removing intersymbol interference includes a fixed operation for removing intersymbol interference caused by introduction of a predetermined amount of intersymbol
10 interference, and an adaptive operation for removing intersymbol interference caused by reasons other than introduction of a predetermined amount of intersymbol interference.

27. A method as claimed in any one of claims 13 to 26 wherein transformation involves using mathematical correlations between representations of the data to
15 reduce computational and/or memory requirements of hardware on which the transformation is determined.

28. A method as claimed in any one of claims 13 to 27 including symbol synchronisation involving measuring the correlation between sections of signal, in which pilot tones are provided on subcarriers.

20 29. A method as claimed in claim 28 in which relative values of the pilot tones on successive symbols follows the sequence +1, 0, +1, 0, -1, 0, -1, 0.

30. A method as claimed in any one of claims 13 to 29 including frequency synchronisation involving measuring phase changes between the pilot tones provided on subcarriers.

25 31. A method as claimed in any one of claims 13 to 27 including frequency synchronisation involving calculating a metric having a known dependence on

frequency offset.

32. A method as claimed in any claim 31 wherein the metric approximates the multiplicative product of frequency offset and symbol period, and is calculated using the expression:

5
$$\operatorname{Re}\left(\frac{y_{k,i} + y_{k+1,i}}{y_{k,i} - y_{k+1,i}}\right)$$

33. A transmitter suitable for transmitting data in a multicarrier modulation system in which transform pairs allow communication using multiple subcarriers, the transmitter including:

means for modulating representations of data on groups of subcarriers; and

10 means for introducing a predetermined amount of intersymbol interference between symbols.

34. A receiver suitable for receiving data in a multicarrier modulation system in which transform pairs allow communication using multiple subcarriers, the receiver including:

15 means for demodulating data from representations of data on groups of subcarriers; and

means for removing a predetermined amount of intersymbol interference between symbols.

35. A multicarrier modulation system incorporating one or more transmitters as
20 claimed in claim 33 and one or more receivers as claimed in claim 34 wherein the transmitters and receivers are adapted to communicate with each other.

FIG. 1

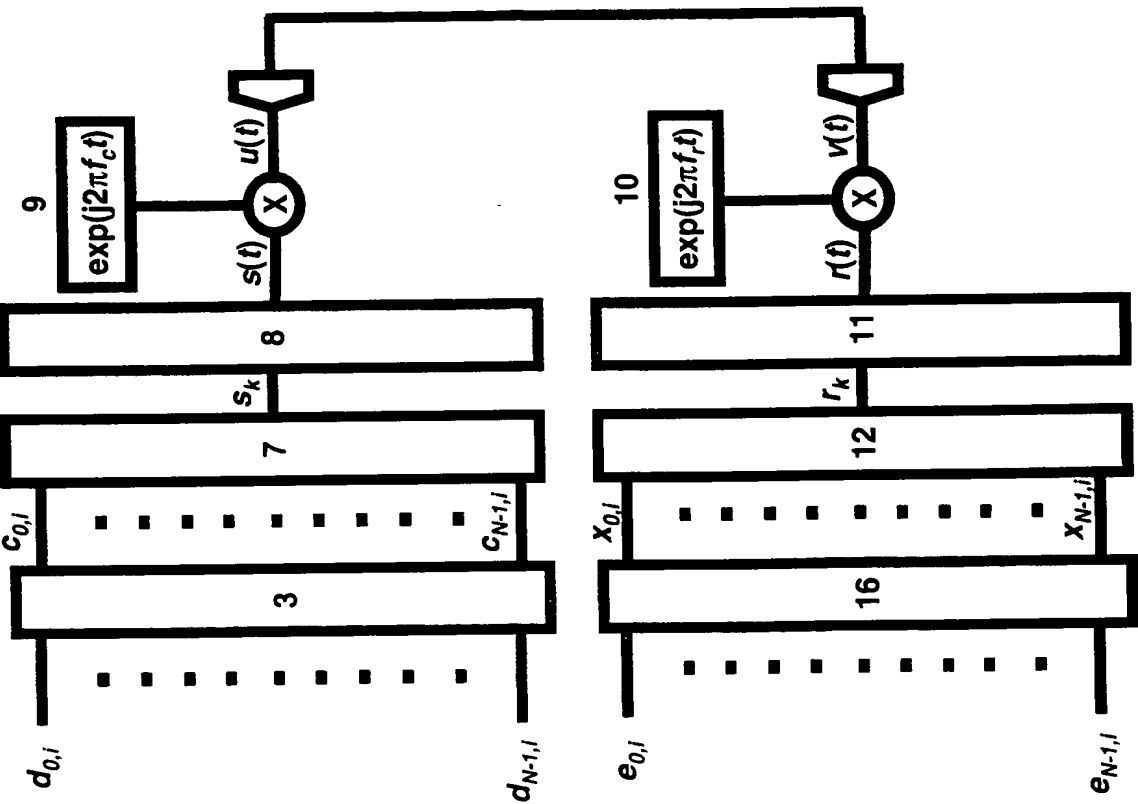


FIG. 2

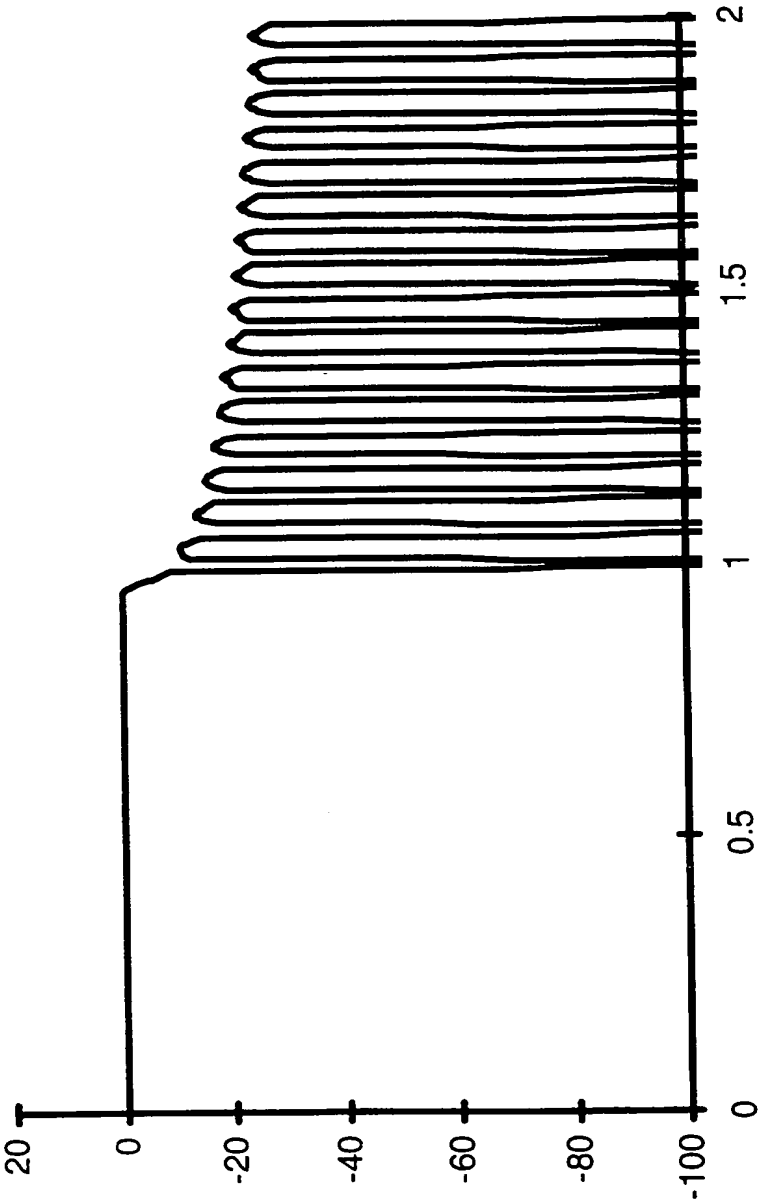
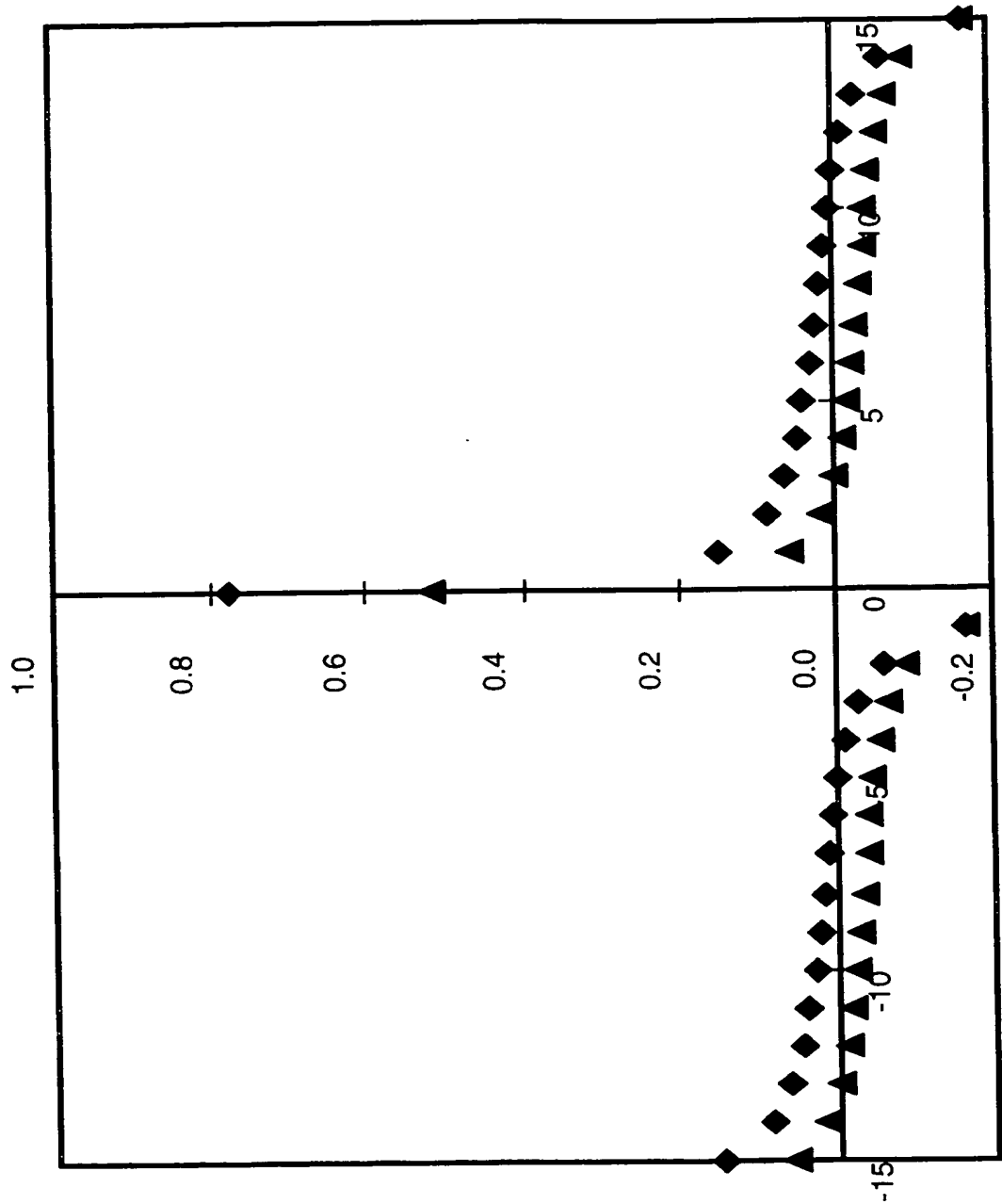
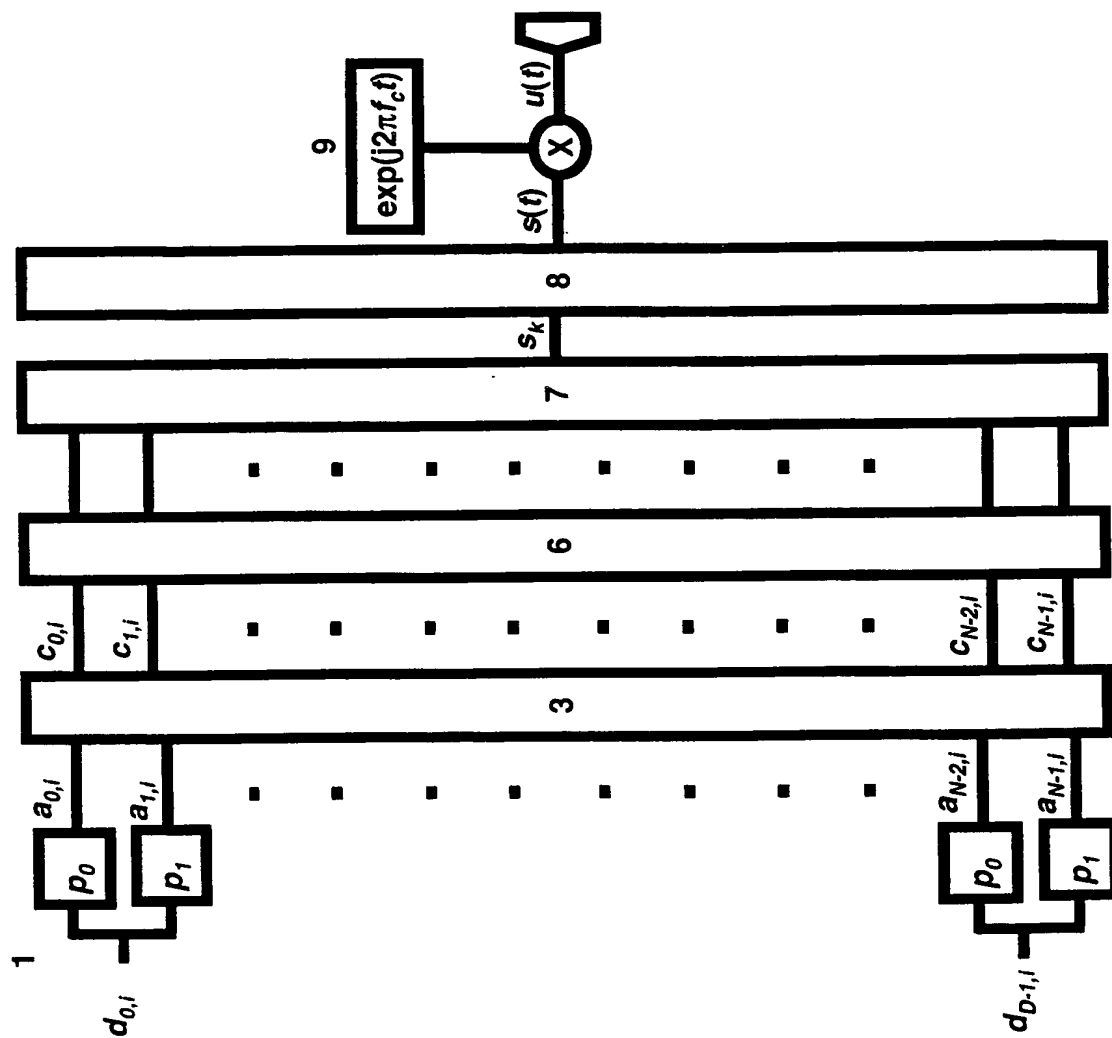


FIG. 3



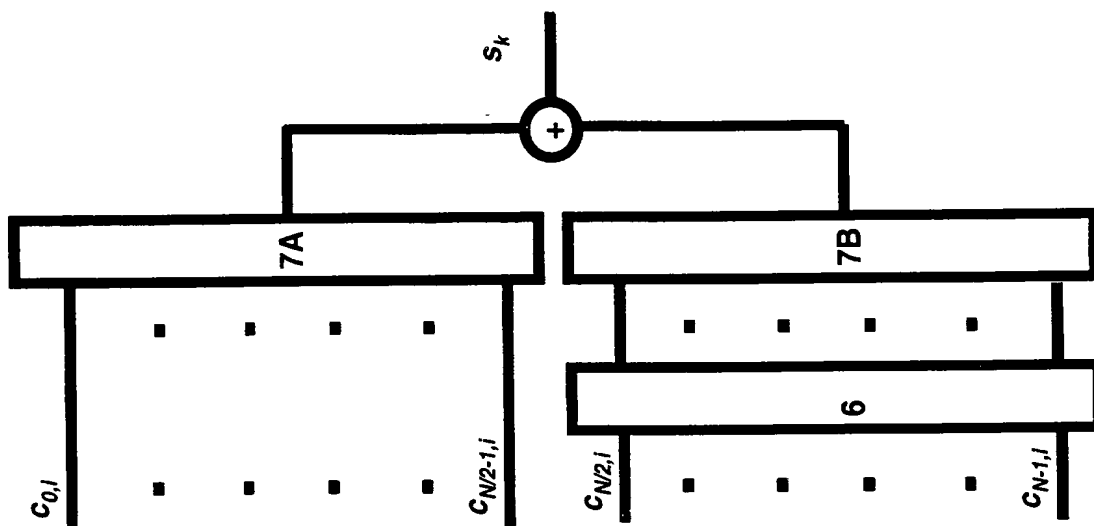
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FIG. 4



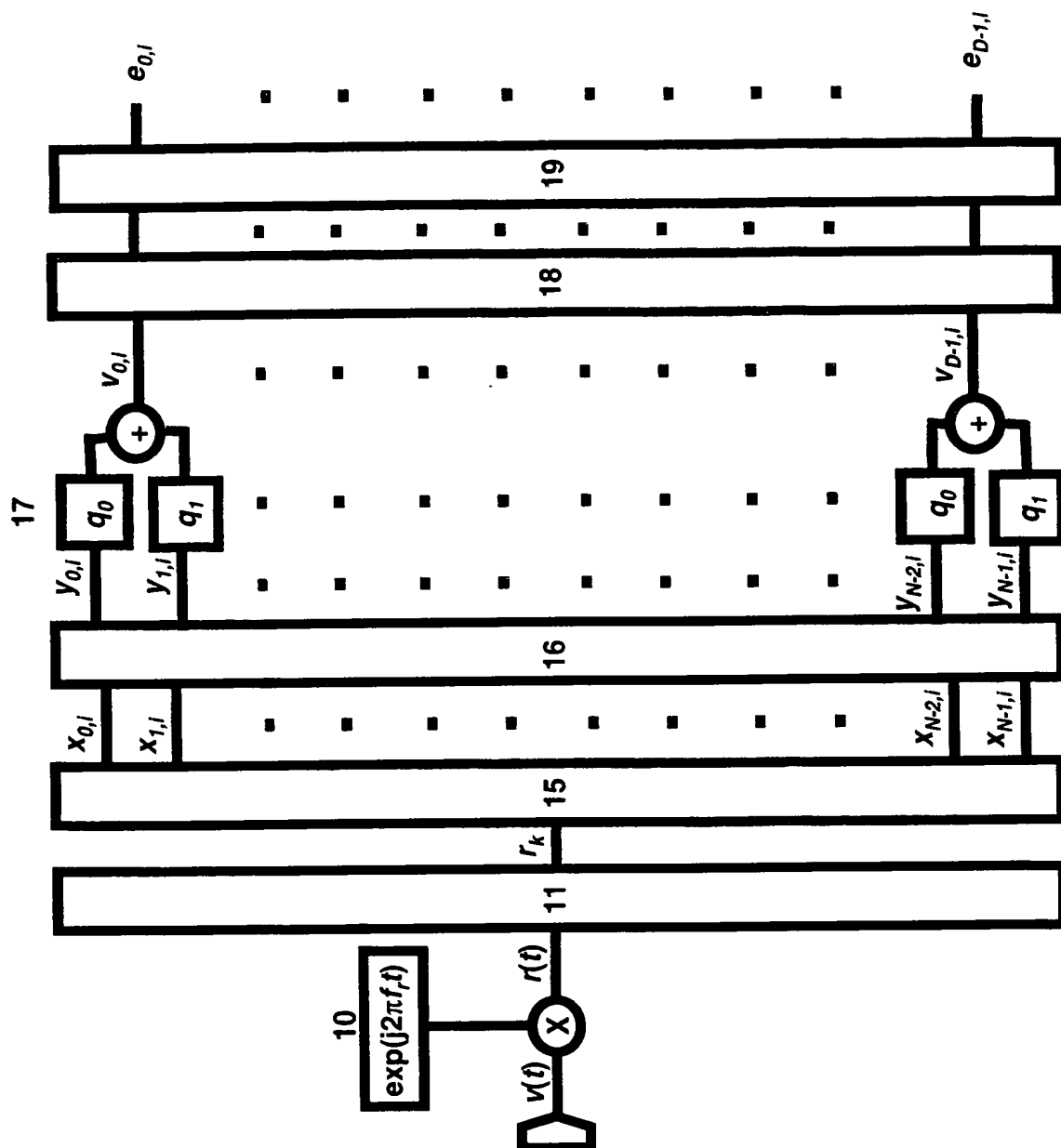
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FIG. 5



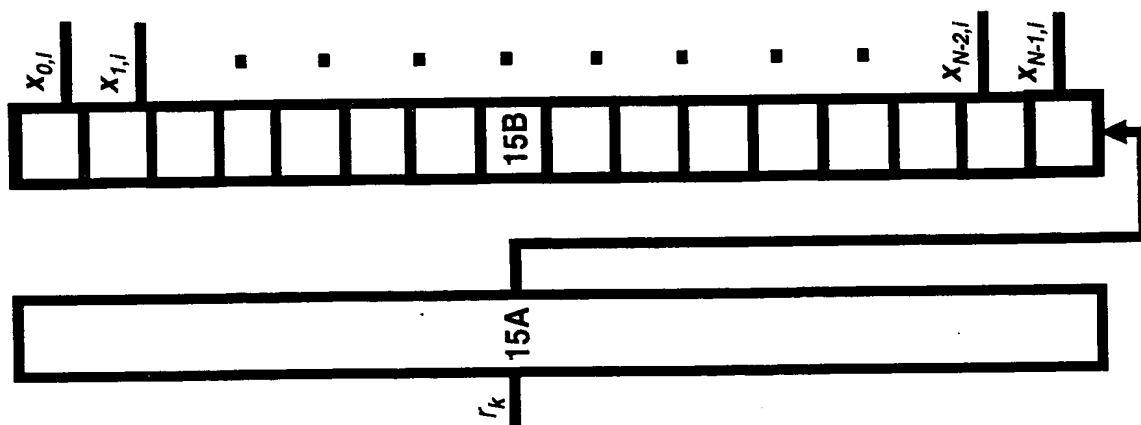
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FIG. 6

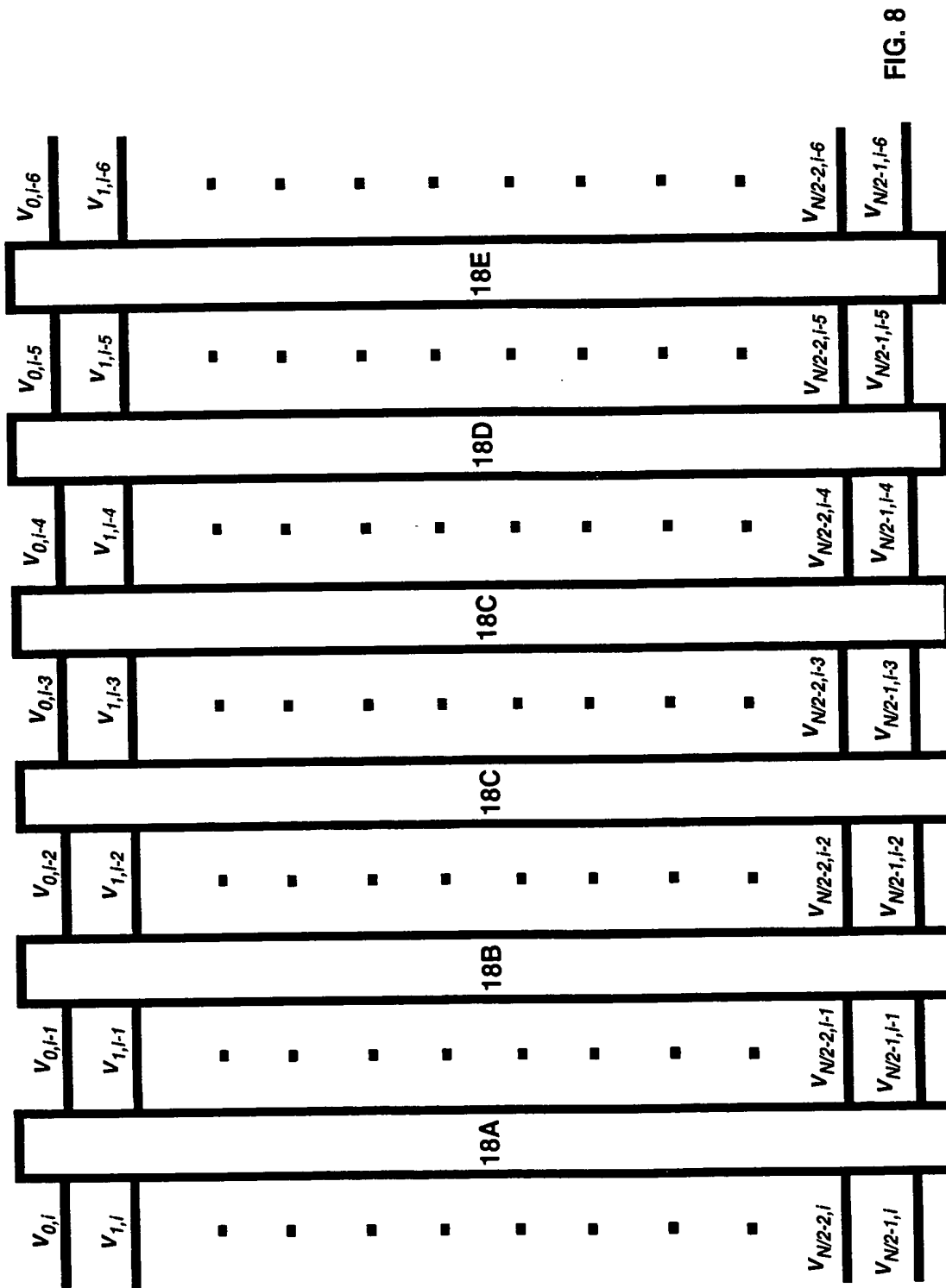


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FIG. 7

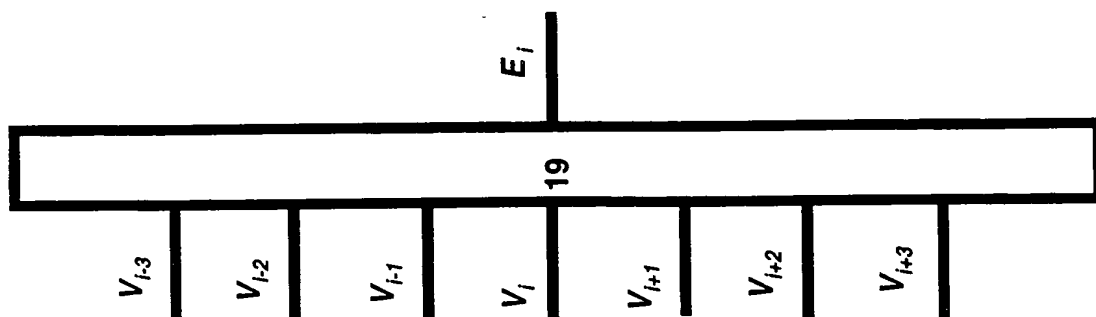


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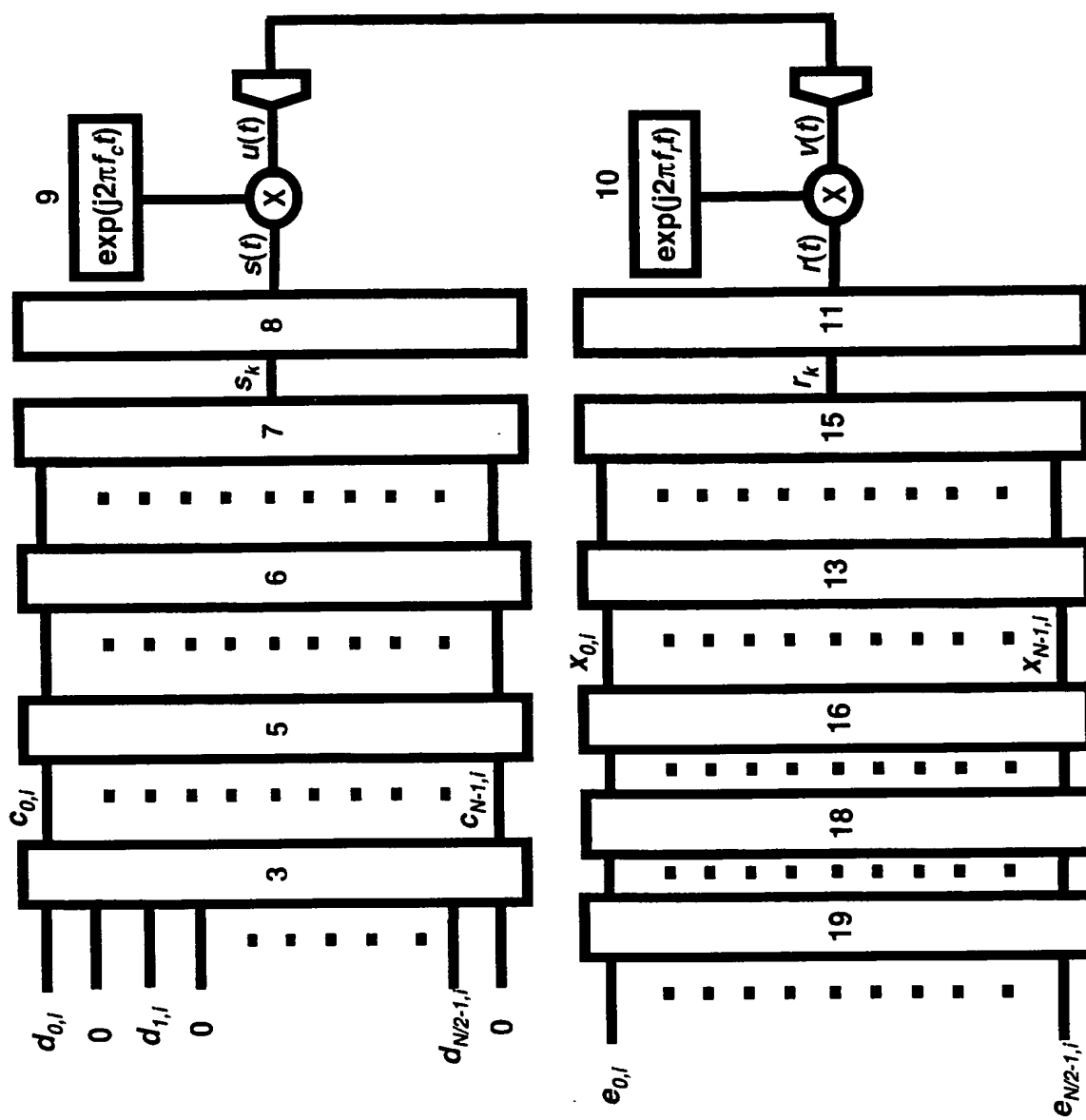
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FIG. 9



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FIG. 10



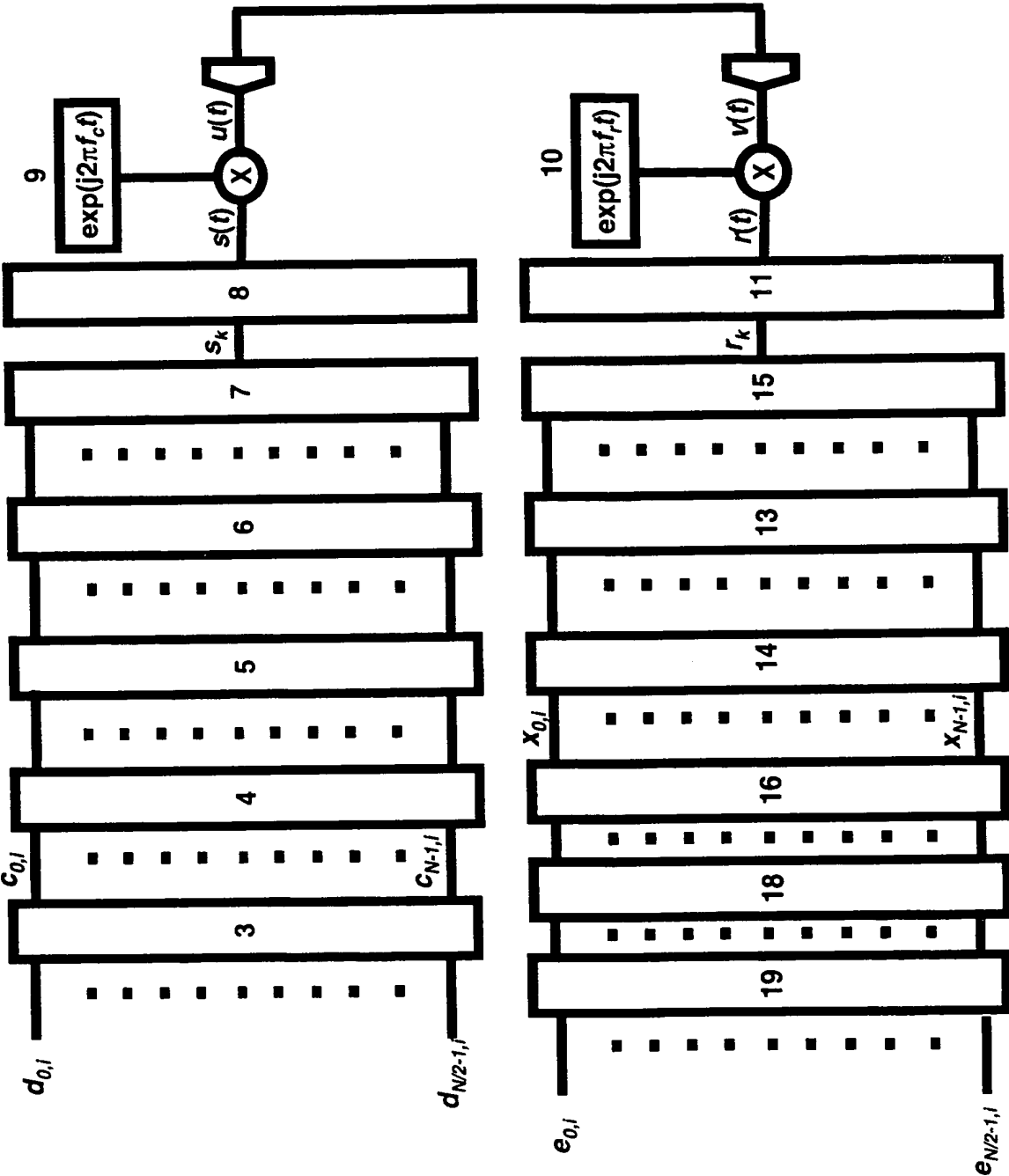
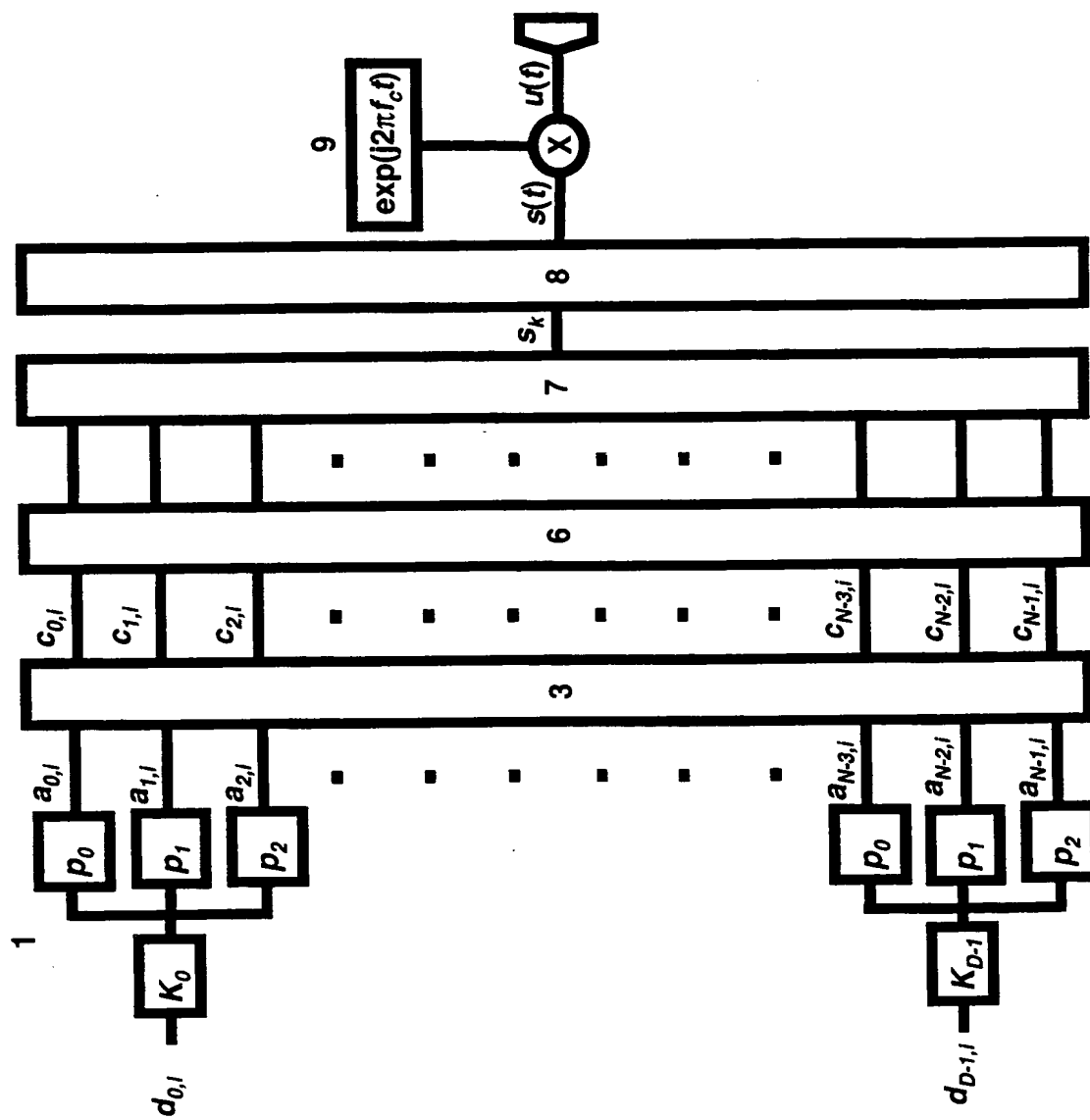


FIG. 11

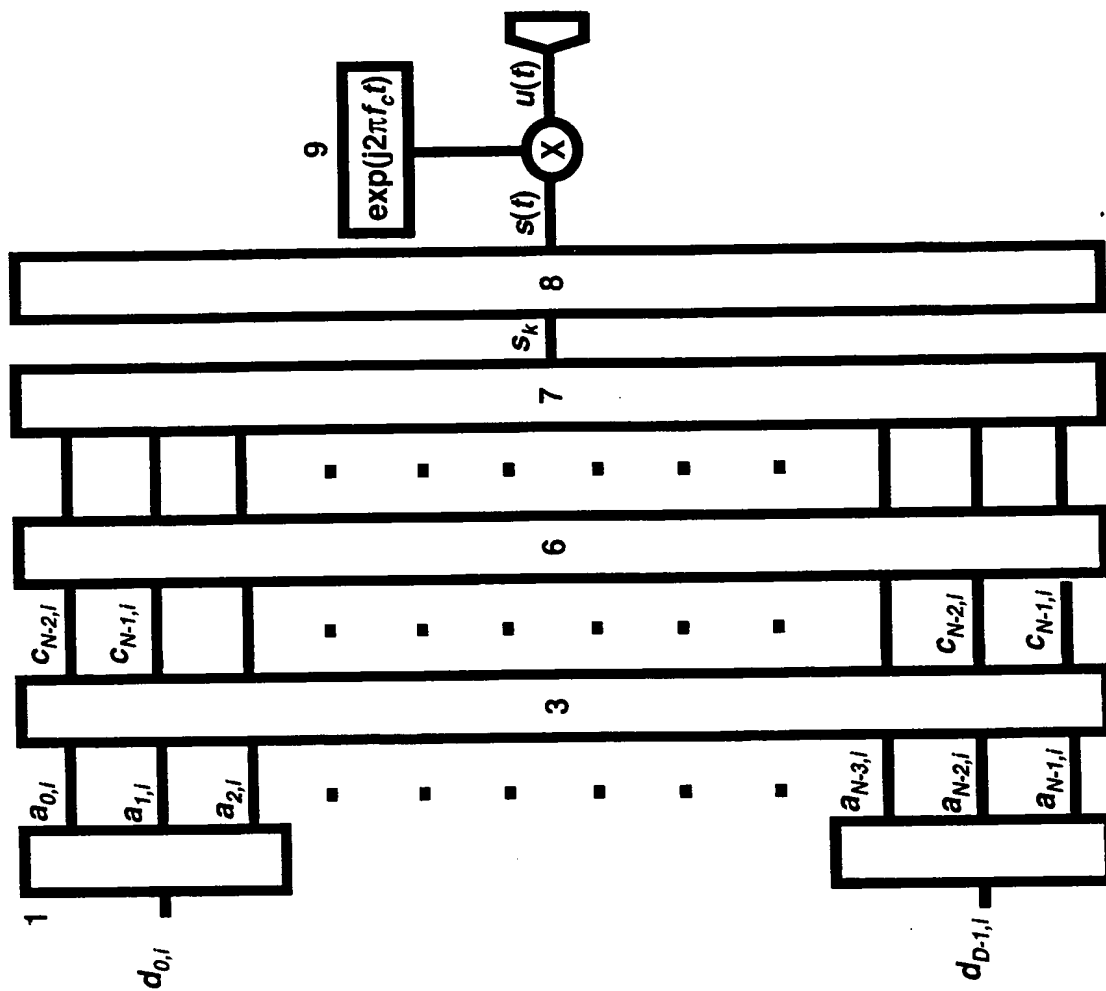
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FIG. 12



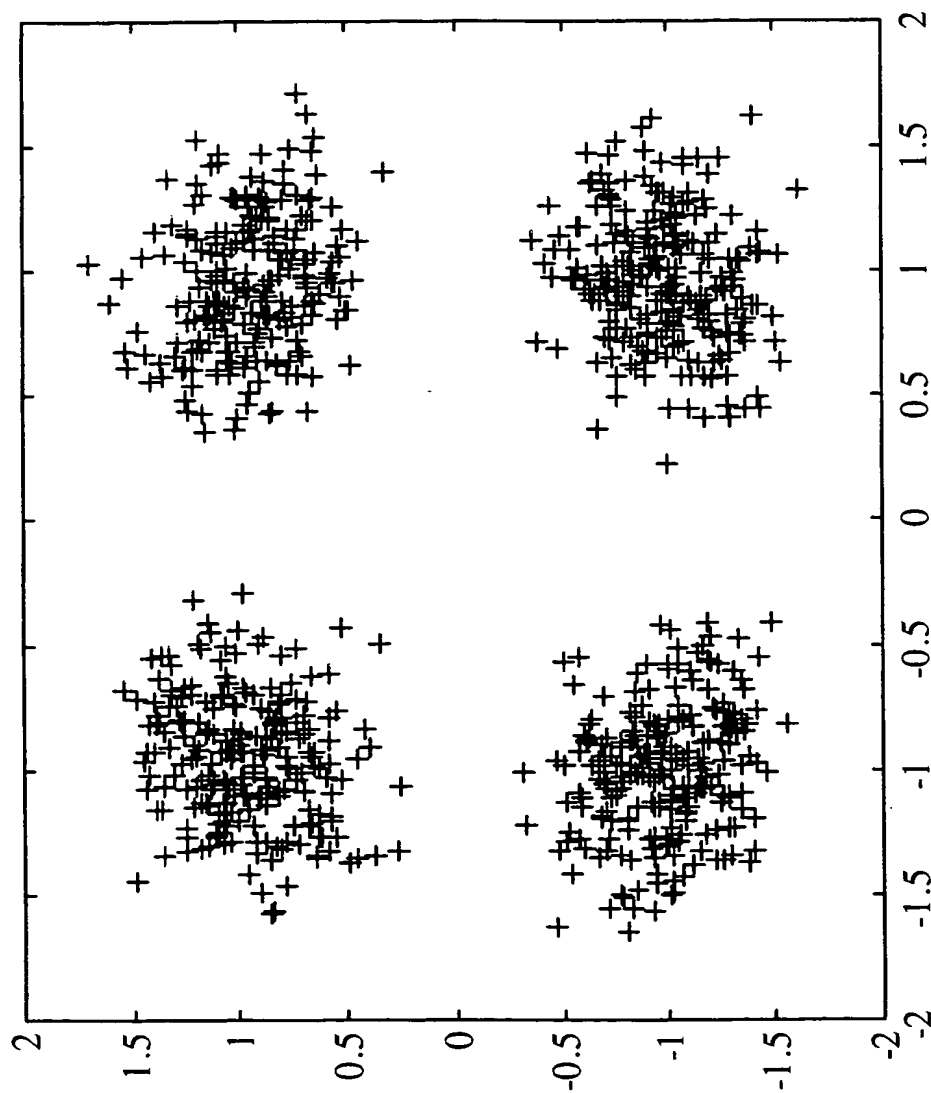
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FIG. 13



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FIG. 14



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FIG. 15

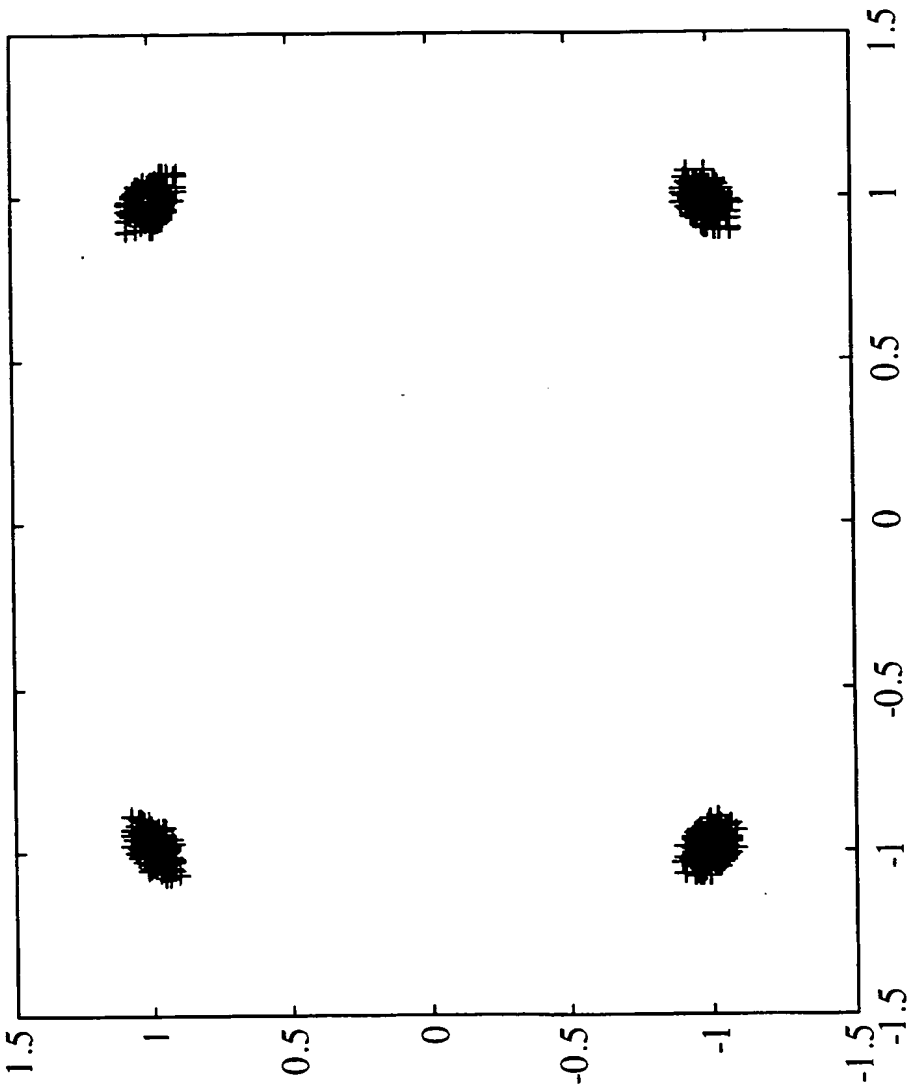
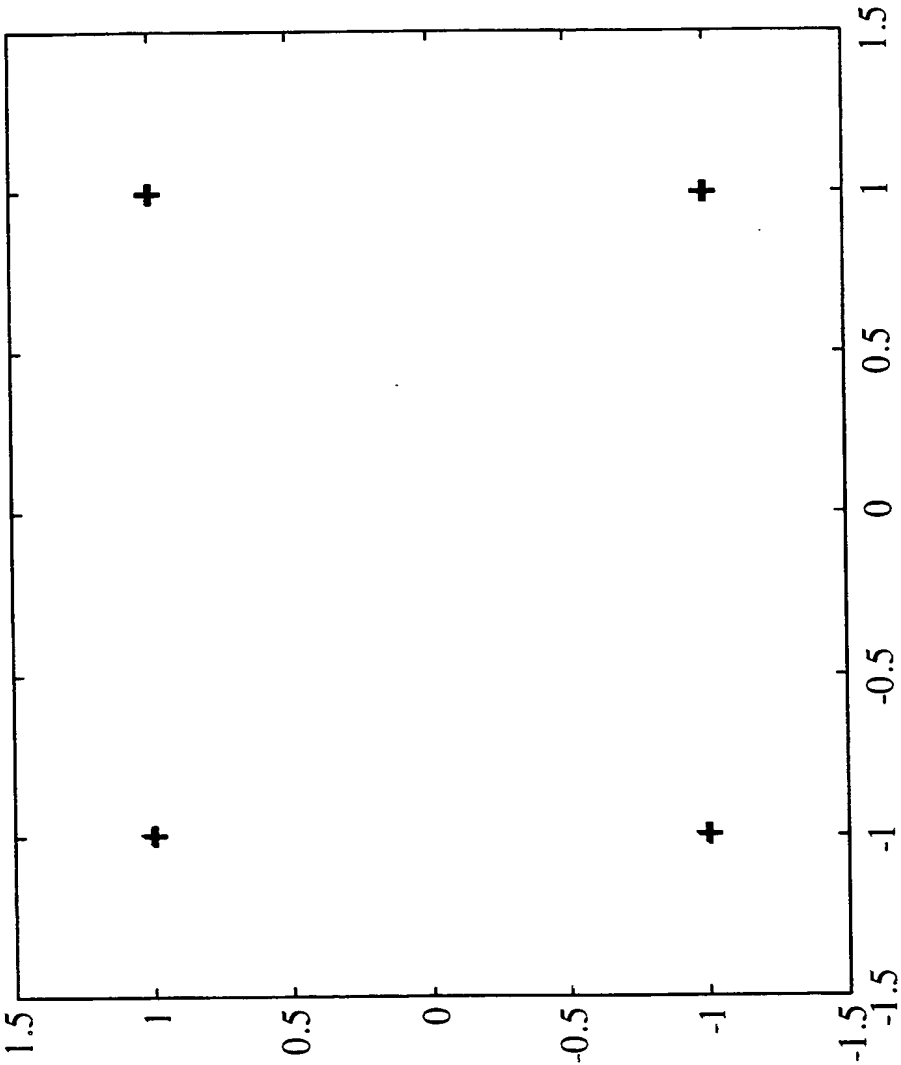


FIG. 16



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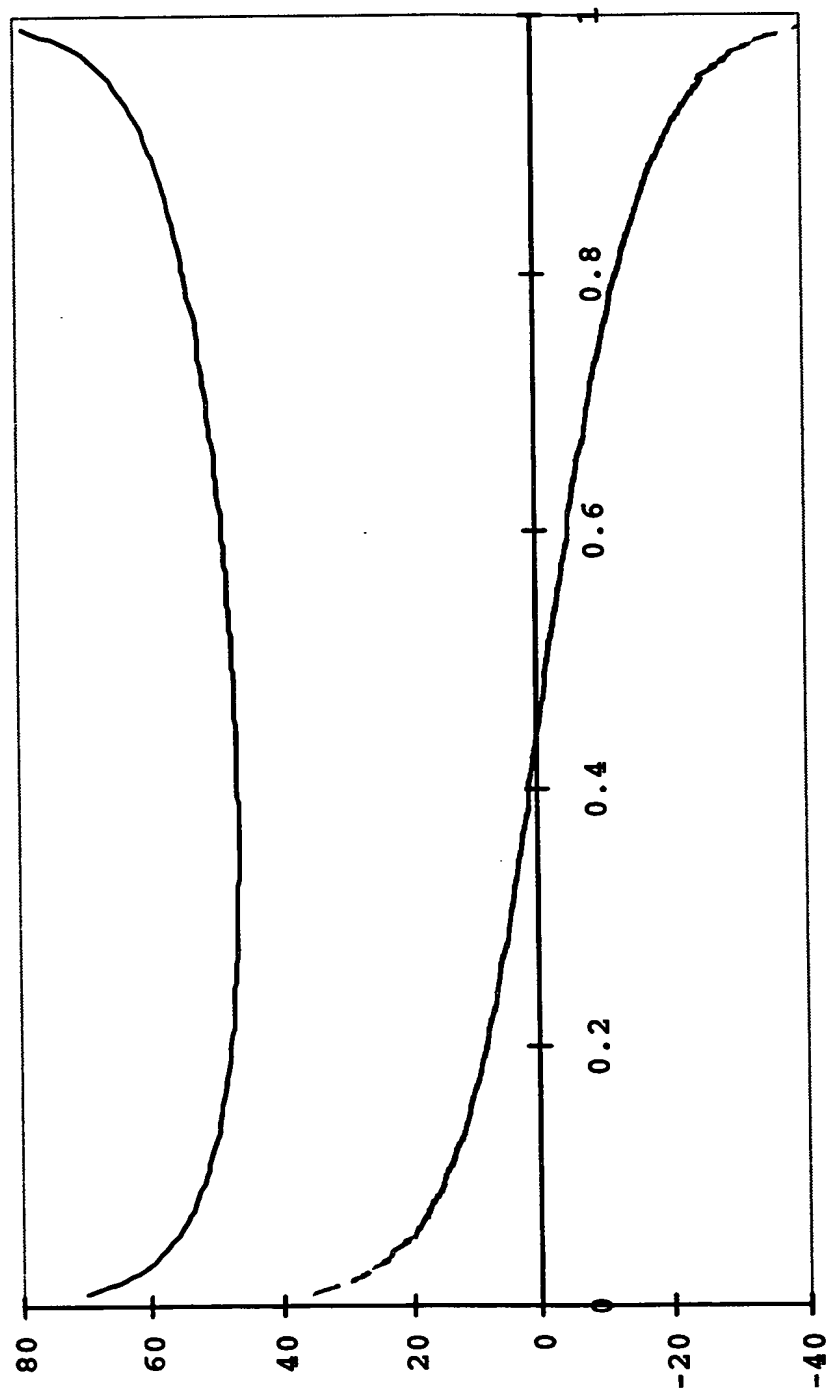
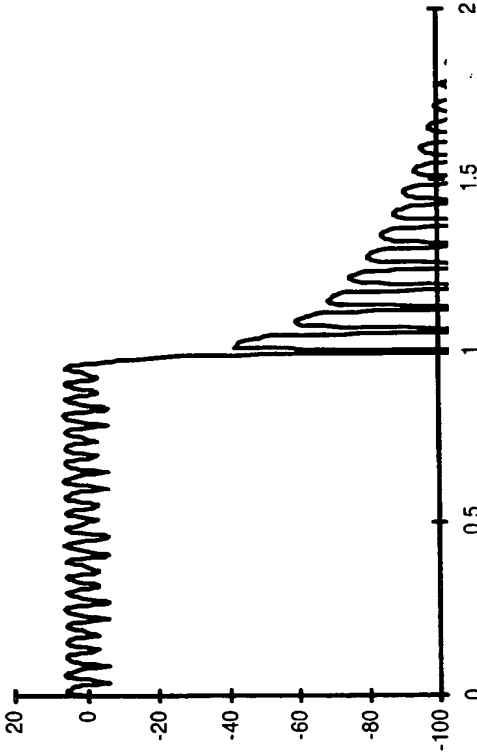
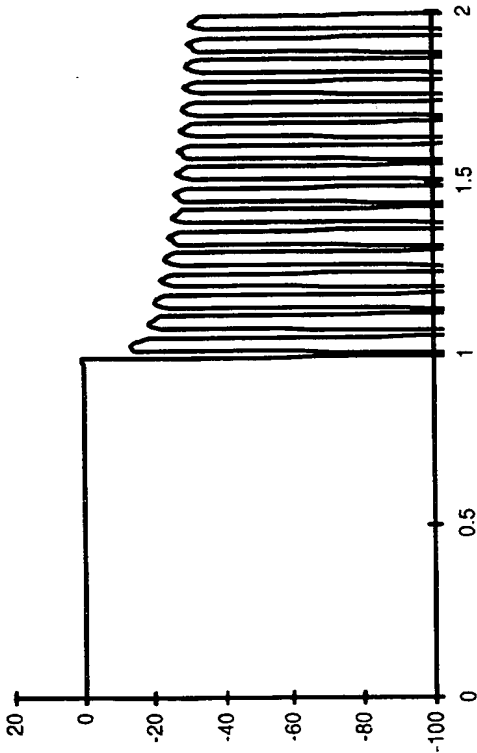


FIG. 17

FIG. 18



INTERNATIONAL SEARCH REPORT

International application No.

PCT/AU 99/00409

A. CLASSIFICATION OF SUBJECT MATTER																						
Int Cl ⁶ : H04J 11/00, 13/00, H04B 7/204, H04L 27/00																						
According to International Patent Classification (IPC) or to both national classification and IPC																						
B. FIELDS SEARCHED																						
Minimum documentation searched (classification system followed by classification symbols) IPC H04J/IC, HO4B/IC, HO4L/IC																						
Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched AU: IPC as above																						
Electronic data base consulted during the international search (name of data base and, where practicable, search terms used) WPAT: (MULTICARRIER()MODULATION# OR MULTICARRIER()SYSTEM#) JAPIO: (MULTICARRIER()MODULATION# OR MULTICARRIER()SYSTEM#)																						
C. DOCUMENTS CONSIDERED TO BE RELEVANT																						
Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.																				
A	US 5068874 A (LEITCH) 26 November 1991 Col. 1 line 61 - col. 6 line 64	1 - 35																				
A	US 5394110 A (MIZOGUCHI) 28 February 1995 Col. 3 line 22 - Col. 7 line 66	1 - 35																				
A	US 5633893 A (LAMPE et al.) 27 May 1997 Col. 1 Line 12 - Col. 7 line 4	1 - 35																				
<input checked="" type="checkbox"/> Further documents are listed in the continuation of Box C <input checked="" type="checkbox"/> See patent family annex																						
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Date of the actual completion of the international search 21 June 1999		Date of mailing of the international search report 13 JUL 1999																				
Name and mailing address of the ISA/AU AUSTRALIAN PATENT OFFICE PO BOX 200 WODEN ACT 2606 AUSTRALIA Facsimile No.: (02) 6285 3929		Authorized officer JUZER KHANBHAI Telephone No.: (02) 6283 2176																				

INTERNATIONAL SEARCH REPORT

international application No.

PCT/AU 99/00409

C (Continuation). DOCUMENTS CONSIDERED TO BE RELEVANT		
Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
A	EP 0838928 A2 (RAI RADIOTELEVISIONE ITALIANA (Sp.A)) 29 April 1998 Page 4 line 39 - Page 9 line 11	1 - 35
P,A	EP 0874494 A2 (AT & T CORP.) 28 October 1998 Col. 1 line 47 - Col. 6 line 16	1 - 35
P,A	WO 99/05798 A1 (KONINKLIJKE PHILIPS ELECTRONIC N.V.) 4 February 1999 Page 2 line 20 - page 11 line 2	1 - 35

INTERNATIONAL SEARCH REPORT

Information on patent family members

International application No.
PCT/AU 99/00409

This Annex lists the known "A" publication level patent family members relating to the patent documents cited in the above-mentioned international search report. The Australian Patent Office is in no way liable for these particulars which are merely given for the purpose of information.

Patent Document Cited in Search Report				Patent Family Member			
US	5068874	EP	572376	WO	91/02403	US	5202900
US	5394110	EP	609828	JP	6 - 232774		
US	5633893	AU	36840/95	CA	2177583	CN	1138397
		SE	9602001	WO	96/10310		
EP	0838928	IT	960867				
EP	0874494	CN	1193228	JP	10 - 294712		
WO	99/05798	NONE					
							END OF ANNEX